

« Advances and Challenges in Static Program Analysis by Abstract Interpretation »

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1. Motivation



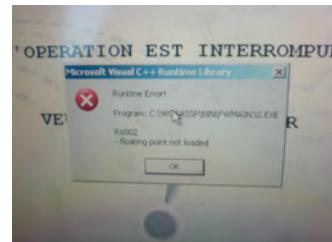
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Bugs Now Show-Up in Everyday Life

- Bugs now appear frequently in everyday life (banks, cars, telephones, ...)
- Example (HSBC bank ATM¹ at 19 Boulevard Sébastopol in Paris, failure on Nov. 21st 2006 at 8:30 am):



¹ cash machine, cash dispenser, automatic teller machine.



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A Strong Need for Software Better Quality

- Poor software quality is not acceptable in safety and mission critical software applications.



- The present state of the art in software engineering does not offer sufficient quality guarantees



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The Complexity of Software Design

- The **design of complex software** is difficult and economically critical
- Example (www.designnews.com/article/CA6475332.html):
“Boeing Confirms 787 Delay, Fasteners, Flight Control Software Code Blamed
John Dodge, Editor-in-Chief – Design News, September 5, 2007

Boeing officials confirmed today that a fastener shortage and problems with flight control software have pushed “first flight” of the Boeing 787 Dreamliner to sometime between mid-November and mid-December (see News Releases).

...

The software delays involve Honeywell Aerospace, which is responsible for flight control software. **The work on this part of the 787 was simply underestimated**, said Bair.”



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Tool-Based Software Design Methods

- New **tool-based software design methods** will have to emerge to face the unprecedented **growth and complexification of critical software**
- E.g. FCPC (Flight Control Primary Computer)
 - A220: 20 000 LOCs,
 - A340 (V1): 130 000 LOCS
 - A340 (V2): 250 000 LOCS
 - A380: 1.000.000 LOCS
 - A350: static analysis to be integrated in the software production



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The Security of Complex Software

- **Complex software** is subject to **security vulnerabilities**
- Example (www.wired.com/politics/security/news/2008/01/dreamliner_security)
“FAA: Boeing’s New 787 May Be Vulnerable to Hacker Attack
Kim Zetter, freelance journalist in Oakland, CA, Jan. 4, 2008

Boeing’s new 787 Dreamliner passenger jet may have a serious **security vulnerability** in its onboard computer networks ...

According to the FAA document published in the Federal Register (mirrored at Cryptome.org), the vulnerability exists because **the plane’s computer systems connect the passenger network with the flight-safety, control and navigation network**. It also connects to the airline’s business and administrative-support network, which communicates maintenance issues to ground crews.



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Static Analysis

A **static analyzer** is a program that

– takes as **input**:

- a **program** P (written in some given programming language \mathbb{P} with a given semantics $\mathfrak{S}_\mathbb{P}$)
- a **specification** S (implicit $S[P]$ or written in some specification language \mathbb{S} with a given semantics $\mathfrak{S}_\mathbb{S}$)
- **always terminates** and delivers **automatically** as **output**:
- a **diagnosis** on the validity of the program semantics with respect the specification semantics



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Difficulties of Static Analysis

- automatic + infinite state + termination \Rightarrow undecidable!
- for a programming (and a specification) language, not for a given model of a given program:

$$\forall P \in \mathbb{P} : \forall S \in \mathbb{S} : \mathcal{G}_{\mathbb{P}}[P] \subseteq \mathcal{G}_{\mathbb{S}}[P, S]?$$

or, more simply for an *implicit specification* $S[P]$:

$$\forall P \in \mathbb{P} : \mathcal{G}_{\mathbb{P}}[P] \subseteq S[P]?$$



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Problems with Formal Methods

- **Formal specifications** (abstract machines, temporal logic, ...) are costly, complex, error-prone, difficult to maintain, not mastered by casual programmers
- **Formal semantics** of the specification and programming language are inexistant, informal, unrealistic or complex
- **Formal proofs** are partial (static analysis), do not scale up (model checking) or need human assistance (theorem proving & proof assistants)
 \Rightarrow **High costs** (for specification, proof assistance, etc).



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Soundness and Completeness

- **Soundness**: for all $P \in \mathbb{P}$, if the answer is yes (no) then $\mathcal{G}_{\mathbb{P}}[P] \subseteq S[P]$ (resp. $\mathcal{G}_{\mathbb{P}}[P] \not\subseteq S[P]$)
- **Completeness**: for all $P \in \mathbb{P}$, if $\mathcal{G}_{\mathbb{P}}[P] \subseteq S[P]$ ($\mathcal{G}_{\mathbb{P}}[P] \not\subseteq S[P]$) then the answer is yes (resp. no)

We always require SOUNDNESS!

Undecidability \Rightarrow NO completeness



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Advantages of Static Analysis

- **Formal specifications** are implicit (no need for explicit, user-provided specifications)
- **Formal semantics** are approximated by the static analyzer (no user-provided models of the program)
- **Formal proofs** are automatic (no required user-interaction)
- **Costs** are low (no modification of the software production methodology)
- **Scales up** to 100.000 to 1.000.000 LOCS
- **Rapid and large diffusion** in embedded software production industries



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Disadvantages of Static Analysis

- **Imprecision** (acceptable in some applications like WCET or program optimization)
- **Incomplete** for program verification
- **False alarms** are due to **unsuccessful automatic proofs** in 5 to 15% of the cases

For example, 1% of 500.000 potential (true or false) alarms is 5.000, too much to be handled by hand!



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2. Informal Introduction to Abstract Interpretation



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Remedies to False Alarms in ASTRÉE

- ASTRÉE is specialized to **specific program properties**²
- ASTRÉE is specialized to **real-time synchronous control/command programs written in C**
- ASTRÉE offers possibilities of **refinement**³

The cost of adapting ASTRÉE to a specific program, should be a small fraction of the cost to test the specific program properties verified by ASTRÉE.

² proof of absence of runtime errors

³ parametrizations and analysis directives



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Abstract Interpretation

There are two **fundamental concepts** in computer science (and in sciences in general) :

- **Abstraction** : to reason on complex systems
- **Approximation** : to make effective undecidable computations

These concepts are formalized by **abstract interpretation** [CC77, Cou78, CC79, Cou81, CC92a]

References

[POPL '77] P. Cousot and R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In 4th ACM POPL.

[Thesis '78] P. Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes. Thèse ès sci. math. Grenoble, march 1978.

[POPL '79] P. Cousot & R. Cousot. Systematic design of program analysis frameworks. In 6th ACM POPL.



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Applications of Abstract Interpretation

- Static Program Analysis [CC77], [CH78], [CC79] including Dataflow Analysis; [CC79], [CC00], Set-based Analysis [CC95], Predicate Abstraction [Cou03], ...
- Grammar Analysis and Parsing [CC03];
- Hierarchies of Semantics and Proof Methods [CC92b], [Cou02];
- Typing & Type Inference [Cou97];
- (Abstract) Model Checking [CC00];
- Program Transformation (including program optimization, partial evaluation, etc) [CC02];



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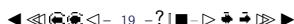


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Principle of Abstraction



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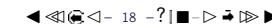
Applications of Abstract Interpretation (Cont'd)

- Software Watermarking [CC04];
- Bisimulations [RT04, RT06];
- Language-based security [GM04];
- Semantics-based obfuscated malware detection [PCJD07].
- Databases [AGM93, BPC01, BS97]
- Computational biology [Dan07]
- Quantum computing [JP06, Per06]

All these techniques involve **sound approximations** that can be formalized by **abstract interpretation**

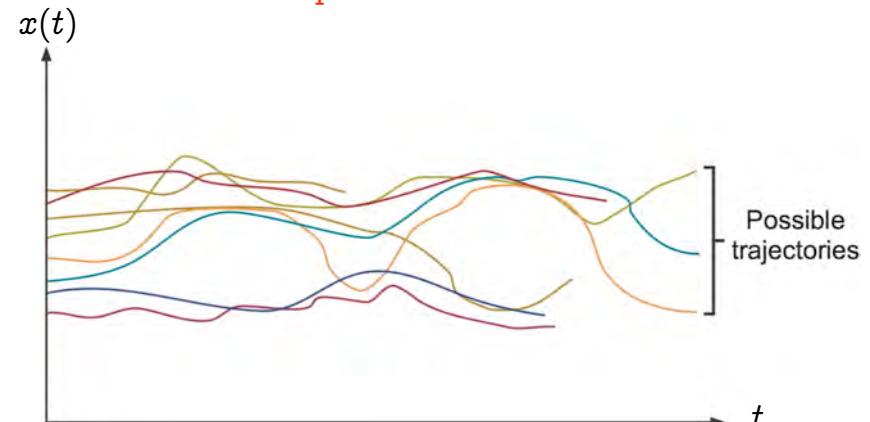


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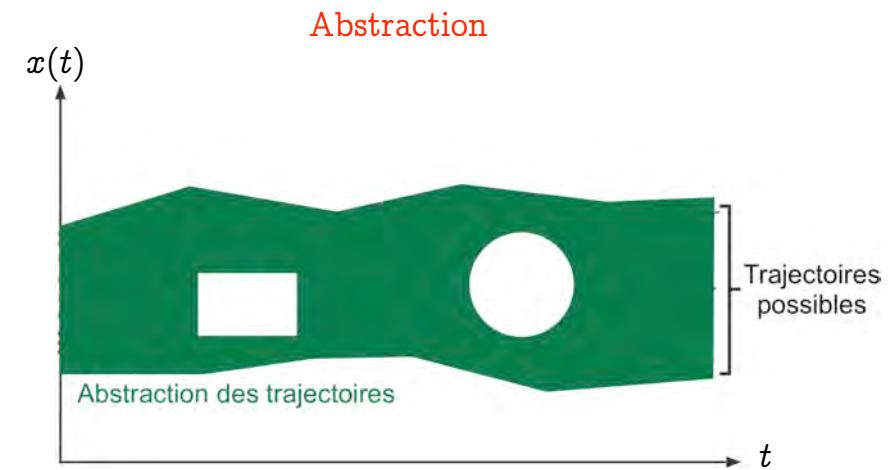
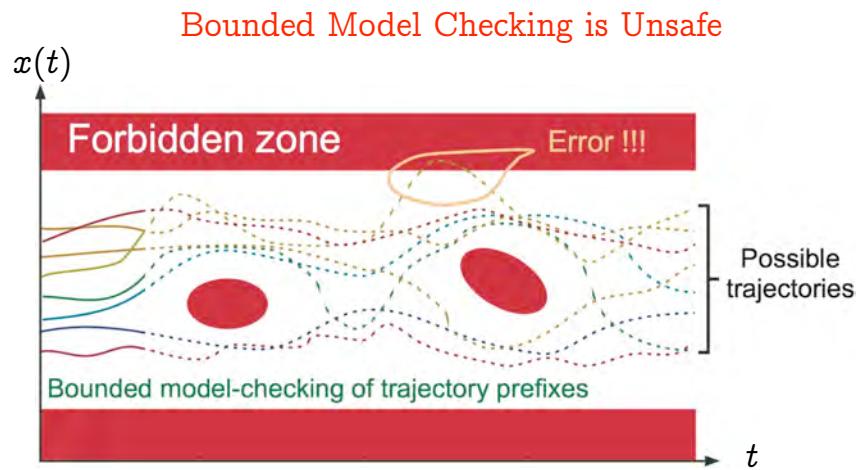
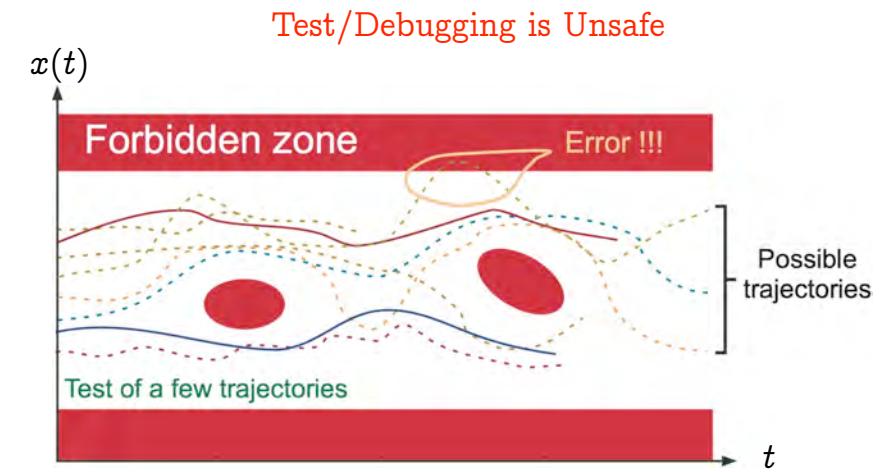
Operational semantics

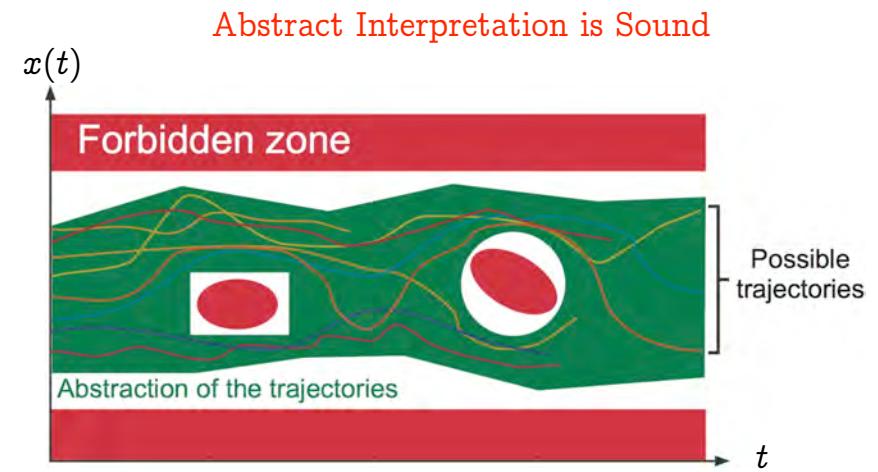
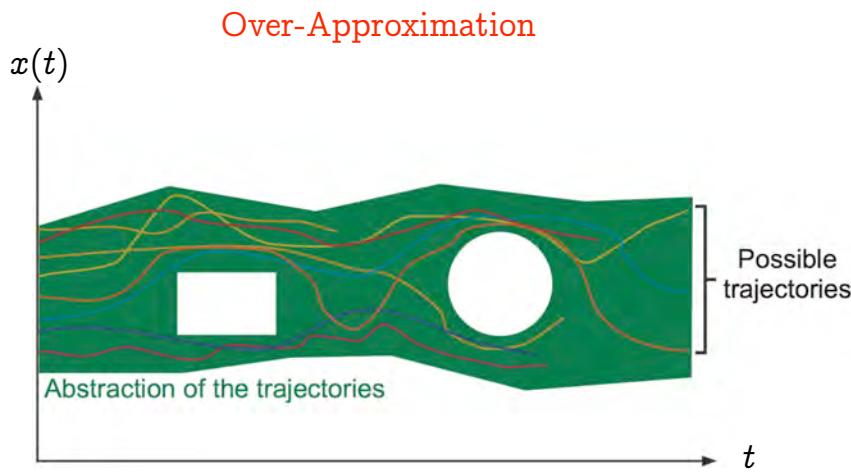


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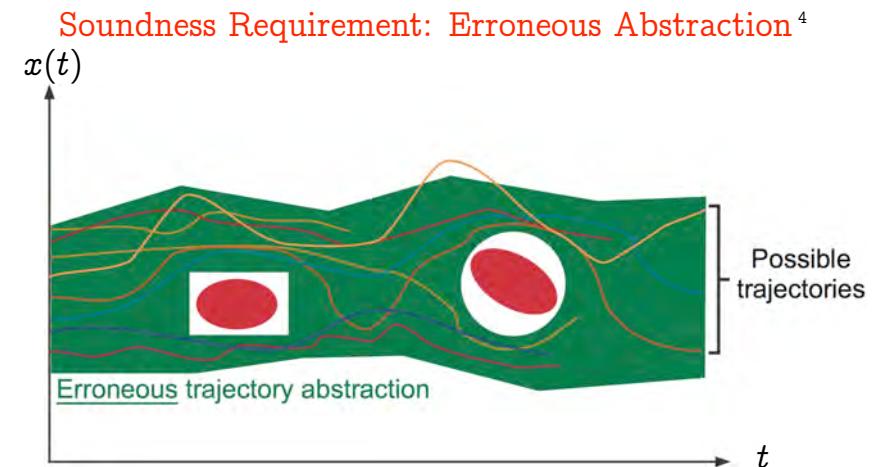


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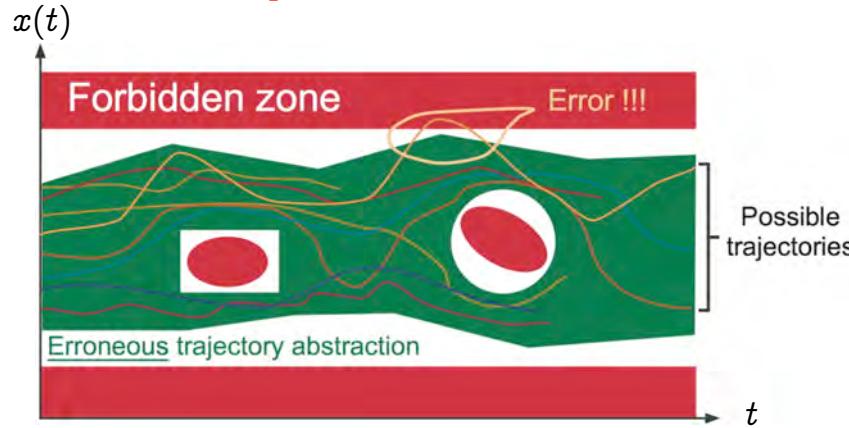


Soundness and Incompleteness



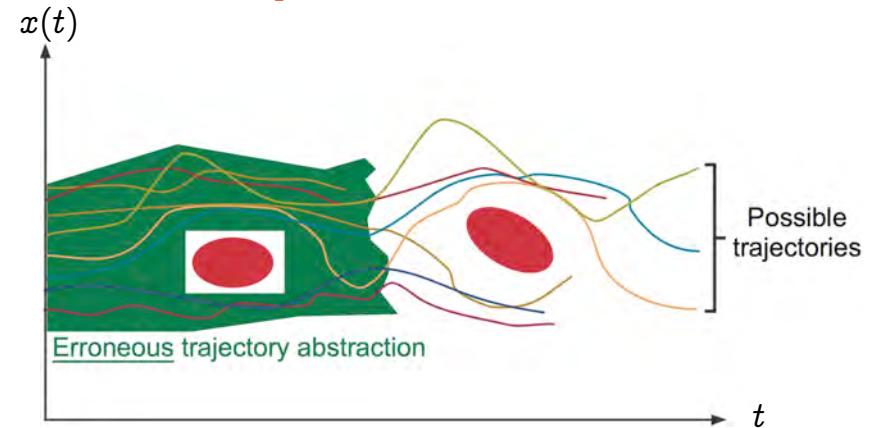
⁴ This situation is always excluded in static analysis by abstract interpretation.

Soundness Requirement: Erroneous Abstraction⁴



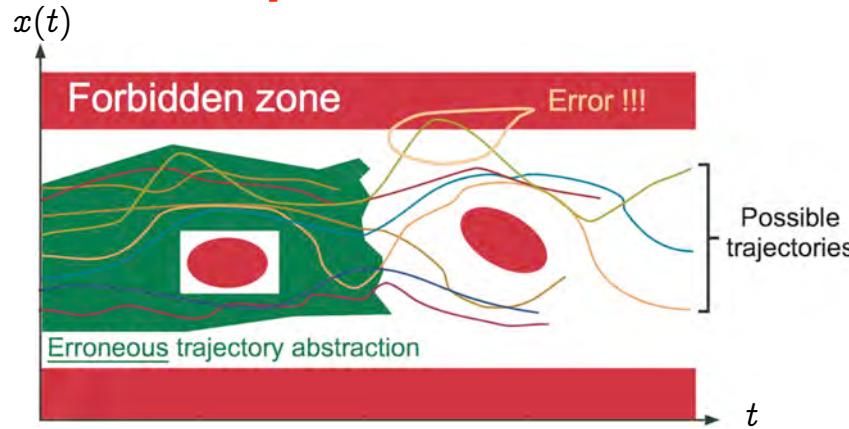
⁴ This situation is always excluded in static analysis by abstract interpretation.

Soundness Requirement: Erroneous Abstraction⁵



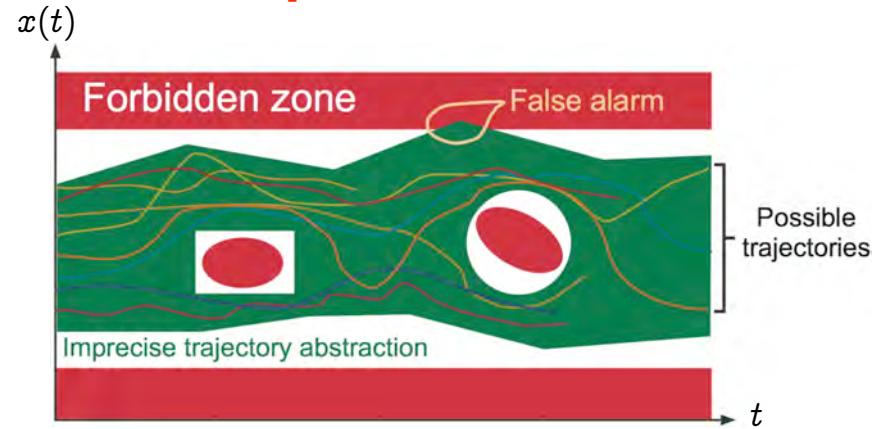
⁵ This situation is always excluded in static analysis by abstract interpretation.

Soundness Requirement: Erroneous Abstraction⁵

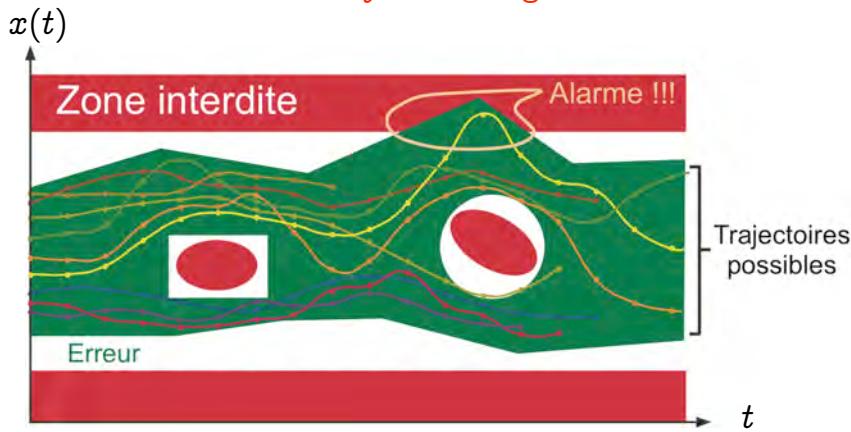


⁵ This situation is always excluded in static analysis by abstract interpretation.

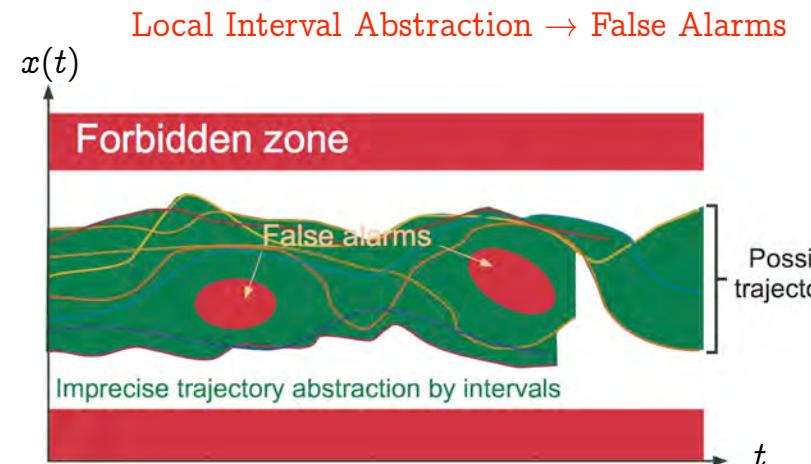
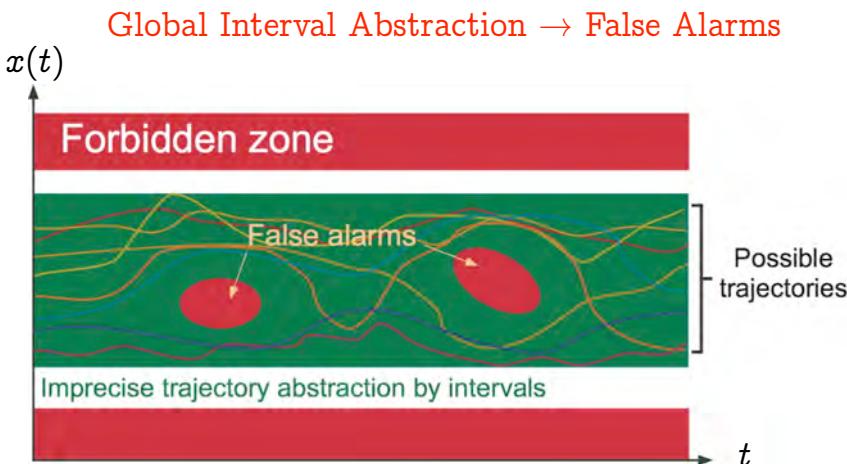
Imprecision ⇒ False Alarms

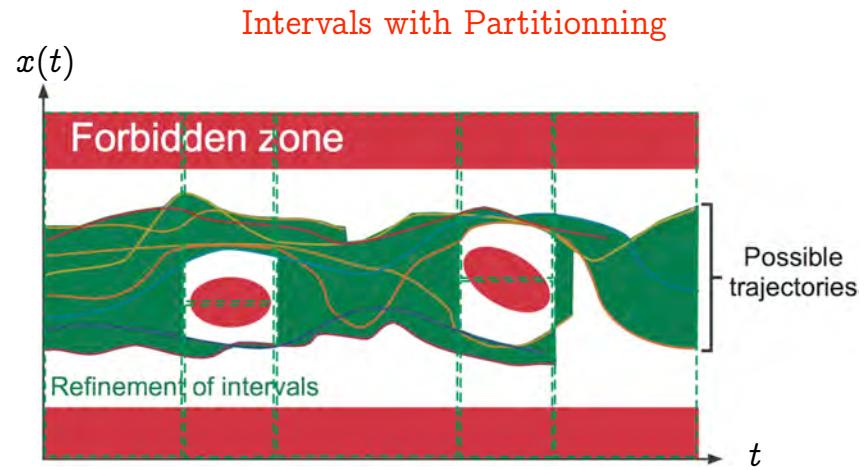
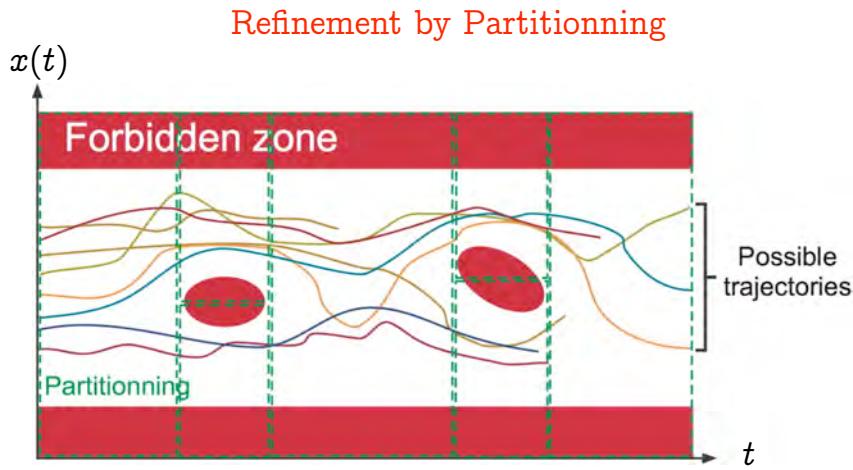


Refinement is necessary to distinguish from true alarms



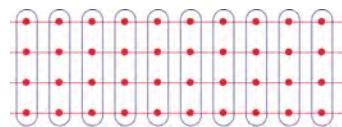
Design by Refinement



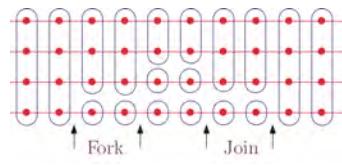


State-based versus Trace-based Partitioning

State-based partitionning at control points:



Trace-based partitionning at control points:



Delaying abstract unions in tests and loops is more precise for non-distributive abstract domains (and much less expensive than disjunctive completion).

Trace Partitioning

Principle:

- Semantic equivalence:

```
if (B) { C1 } else { C2 }; C3
↓
if (B) { C1; C3 } else { C2; C3 };
```

- More precise in the abstract: concrete execution paths are merged later.

Application:

```
if (B)
{ X=0; Y=1; }
else
{ X=1; Y=0; }
R = 1 / (X-Y);
```

cannot result in a division by zero

Case analysis with loop unrolling

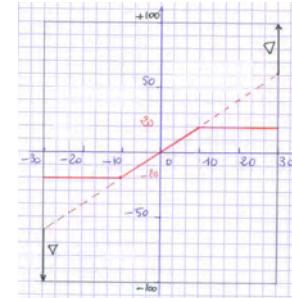
- Code Sample:

```
/* trace_partitionning.c */
void main() {
    float t[5] = {-10.0, -10.0, 0.0, 10.0, 10.0};
    float c[4] = {0.0, 2.0, 2.0, 0.0};
    float d[4] = {-20.0, -20.0, 0.0, 20.0};
    float x, r;
    int i = 0;
    _ASTREE_known_fact((-30.0 <= x) && (x <= 30.0));
    while ((i < 3) && (x >= t[i+1])) {
        i = i + 1;
    }
    r = (x - t[i]) * c[i] + d[i];
    _ASTREE_log_vars((r));
}
```

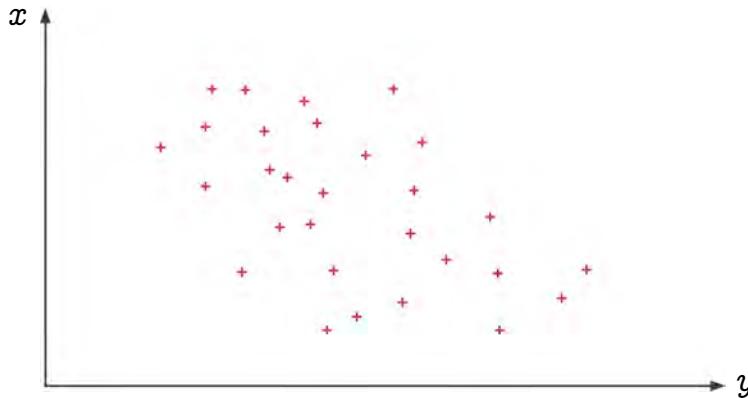
```
% astree -exec-fn main -no-trace -no-relational trace-partitionning.c |& egrep "(WARN)|(r in)"
direct = <float-interval: r in [-20, 20] >
%
% astree -exec-fn main -no-partition -no-trace -no-relational trace-partitionning.c \
|& egrep "(WARN)|(r in)"
direct = <float-interval: r in [-100, 100] >
%
```



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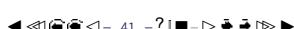
Examples of abstractions



Set of points $\{(x_i, y_i) : i \in \Delta\}$



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Examples of abstractions

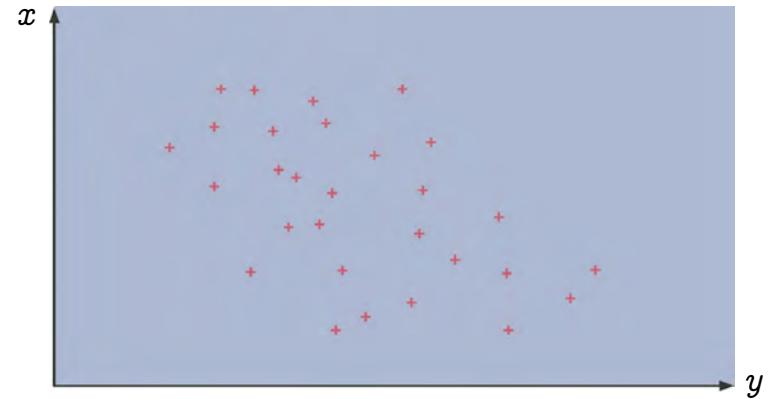


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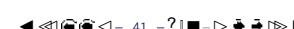
Examples of abstractions



Signs $x \geq 0, y \geq 0$ [CC79]

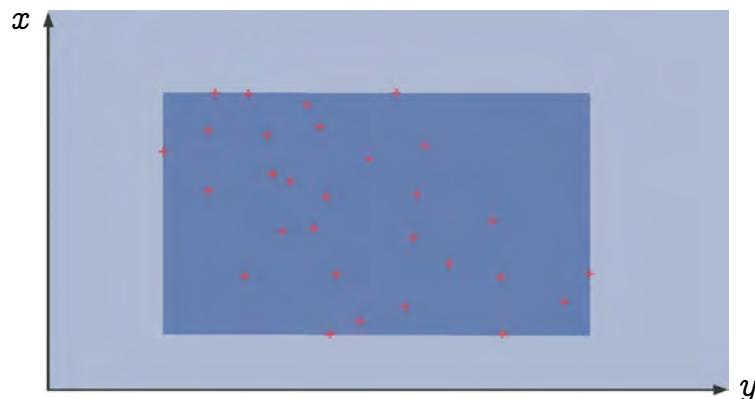


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Examples of abstractions



Intervals $a \leq x \leq b, c \leq y \leq d$ [CC77]

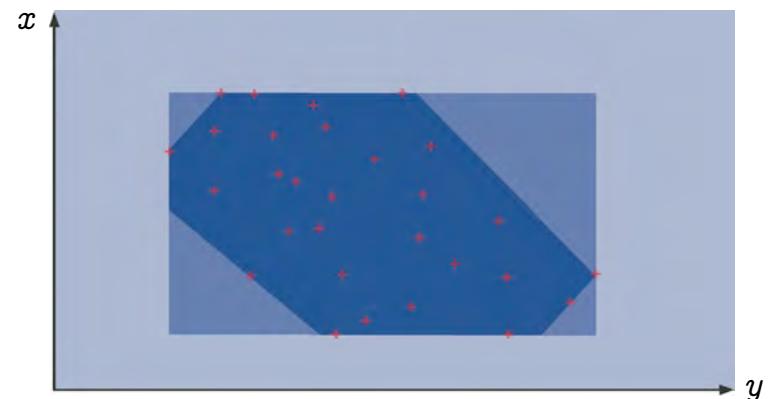


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Examples of abstractions



Octagons $x - y \leq a, x + y \leq b$ [Min06b]

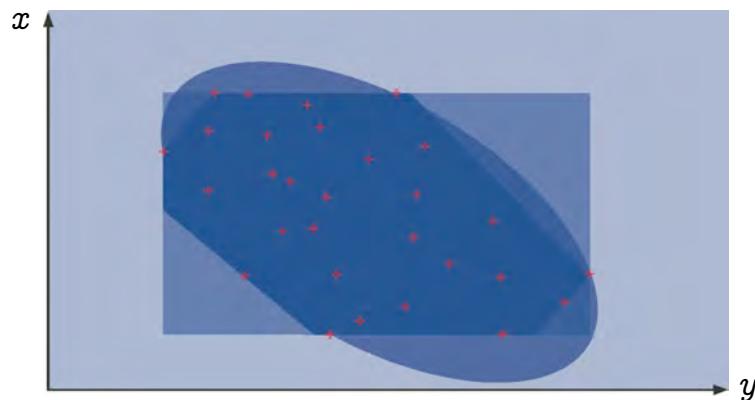


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Examples of abstractions



Ellipsoids $(x - a)^2 + (y - b)^2 \leq c$ [?]

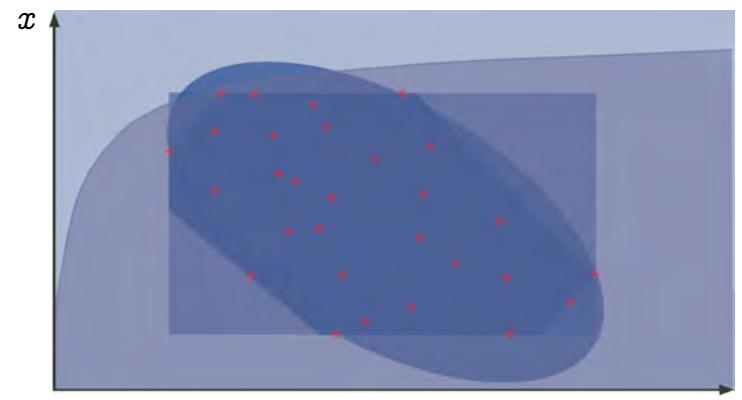


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Examples of abstractions



Exponentials $a^x \leq y$ [Fer05]



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3. The ASTRÉE static analyzer

<http://www.astree.ens.fr/>



Programs Analyzed by ASTRÉE and their Semantics



Project Members



Bruno BLANCHET⁶



Patrick COUSOT



Radhia COUSOT



Jérôme FERET



Laurent MAUBORGNE



Antoine MINÉ



David MONNIAUX⁷



Xavier RIVAL

⁶ Nov. 2001 — Nov. 2003.

⁷ Nov. 2001 — Aug. 2007.



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Programs analysed by ASTRÉE

- Application Domain: large safety critical embedded real-time synchronous software for non-linear control of very complex control/command systems.
- C programs:
 - with
 - basic numeric datatypes, structures and arrays
 - pointers (including on functions),
 - floating point computations
 - tests, loops and function calls
 - limited branching (forward goto, break, continue)



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- with (cont'd) **NEW**
 - union [Min06a]
 - pointer arithmetics & casts [Min06a]
- without
 - dynamic memory allocation
 - recursive function calls
 - unstructured/backward branching
 - conflicting side effects
 - C libraries, system calls (parallelism)

Such limitations are quite common for embedded safety-critical software.

Specification Proved by ASTRÉE

The Class of Considered Periodic Synchronous Programs

```
declare volatile input, state and output variables;
initialize state and output variables;
loop forever
  - read volatile input variables,
  - compute output and state variables,
  - write to output variables;
  __ASTREE_wait_for_clock ();
end loop
```

Task scheduling is static:

- Requirements: the only interrupts are clock ticks;
- Execution time of loop body less than a clock tick, as verified by the ait WCET Analyzers [FHL⁺⁰¹].

Implicit Specification: Absence of Runtime Errors

- No violation of the norm of C (e.g. array index out of bounds, division by zero)
- No implementation-specific undefined behaviors (e.g. maximum short integer is 32767, NaN)
- No violation of the programming guidelines (e.g. static variables cannot be assumed to be initialized to 0)
- No violation of the programmer assertions (must all be statically verified).

Different Classes of Run-time Errors

1. Errors terminating the execution ⁸. ASTRÉE warns and continues by taking into account only the executions that did not trigger the error.
2. Errors not terminating the execution with predictable outcome ⁹. ASTRÉE warns and continues with worst-case assumptions.
3. Errors not terminating the execution with unpredictable outcome¹⁰. ASTRÉE warns and continues by taking into account only the executions that did not trigger the error.

⇒ ASTRÉE is sound with respect to **C standard**, unsound with respect to **C implementation**, unless **no false alarm**.

⁸ floating-point exceptions e.g. (invalid operations, overflows, etc.) when traps are activated

⁹ e.g. overflows over signed integers resulting in some signed integer.

¹⁰ e.g. memory corruptions.

Modular Arithmetic

Modular arithmetic is not very intuitive

In C:

```
% cat -n modulo-c.c
1 #include <stdio.h>
2 int main () {
3 int x,y;
4 x = -2147483647 / -1;
5 y = ((-x) -1) / -1;
6 printf("x = %i, y = %i\n",x,y);
7 }
8
```

```
% gcc modulo-c.c
% ./a.out
x = 2147483647, y =
```

Modular arithmetic is not very intuitive

In C:

```
% cat -n modulo-c.c
1 #include <stdio.h>
2 int main () {
3 int x,y;
4 x = -2147483647 / -1;
5 y = ((-x) -1) / -1;
6 printf("x = %i, y = %i\n",x,y);
7 }
8
```

```
% gcc modulo-c.c
% ./a.out
x = 2147483647, y = -2147483648
```

Static Analysis with ASTRÉE

```
% cat -n modulo.c
 1 int main () {
 2 int x,y;
 3 x = -2147483647 / -1;
 4 y = ((-x) -1) / -1;
 5 __ASTREE_log_vars((x,y));
 6 }
 7

% astree -exec-fn main -unroll 0 modulo.c \
|& egrep -A 1 "(<integers>|WARN)"
modulo.c:4.4-18::[call#main@1]: WARN: signed int arithmetic range
{2147483648} not included in [-2147483648, 2147483647]
<integers (intv+cong+bitfield+set): y in [-2147483648, 2147483647] /\ Top
x in {2147483647} /\ {2147483647} >
```

ASTRÉE signals the overflow and goes on with an unkown value.

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Float Overflow

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Float Arithmetics does Overflow

In C:

```
% cat -n overflow.c
 1 void main () {
 2 double x,y;
 3 x = 1.0e+256 * 1.0e+256;
 4 y = 1.0e+256 * -1.0e+256;
 5 __ASTREE_log_vars((x,y));
 6 }

% gcc overflow.c
% ./a.out
x = inf, y = -inf

% astree -exec-fn main
overflow.c |& grep "WARN"
overflow.c:3.4-23::[call#main1]: 
WARN: double arithmetic range
[1.79769e+308, inf] not
included in [-1.79769e+308,
1.79769e+308]
overflow.c:4.4-24::[call#main1]: 
WARN: double arithmetic range
[-inf, -1.79769e+308] not
included in [-1.79769e+308,
1.79769e+308]
```

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The Ariane 5.01 maiden flight

- June 4th, 1996 was the
maiden flight of Ariane 5



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The Ariane 5.01 maiden flight failure

- June 4th, 1996 was the maiden flight of Ariane 5
- The launcher was destroyed after 40 seconds of flight because of a software overflow¹¹



¹¹ A 16 bit piece of code of Ariane 4 had been reused within the new 32 bit code for Ariane 5. This caused an uncaught overflow, making the launcher uncontrollable.

Rounding

Example of rounding error

```
/* float-error.c */
int main () {
    float x, y, z, r;
    x = 1.000000019e+38;
    y = x + 1.0e21;
    z = x - 1.0e21;
    r = y - z;
    printf("%f\n", r);
}
% gcc float-error.c
% ./a.out
0.000000
```

```
/* double-error.c */
int main () {
    double x; float y, z, r;
    /* x = ldexp(1.,50)+ldexp(1.,26); */
    x = 1125899973951488.0;
    y = x + 1;
    z = x - 1;
    r = y - z;
    printf("%f\n", r);
}
% gcc double-error.c
% ./a.out
134217728.000000
```

$$(x + a) - (x - a) \neq 2a$$

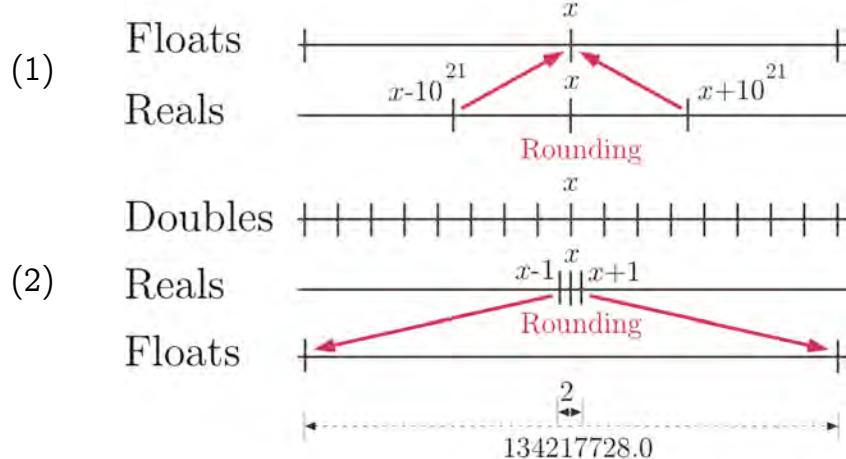
Example of rounding error

```
/* float-error.c */
int main () {
    float x, y, z, r;
    x = 1.000000019e+38;
    y = x + 1.0e21;
    z = x - 1.0e21;
    r = y - z;
    printf("%f\n", r);
}
% gcc float-error.c
% ./a.out
0.000000
```

```
/* double-error.c */
int main () {
    double x; float y, z, r;
    /* x = ldexp(1.,50)+ldexp(1.,26); */
    x = 1125899973951487.0;
    y = x + 1;
    z = x - 1;
    r = y - z;
    printf("%f\n", r);
}
% gcc double-error.c
% ./a.out
0.000000
```

$$(x + a) - (x - a) \neq 2a$$

Explanation of the huge rounding error



Static analysis with ASTRÉE¹²

```
% cat -n double-error.c
 2 int main () {
 3     double x; float y, z, r;;
 4     /* x = ldexp(1.,50)+ldexp(1.,26); */
 5     x = 1125899973951488.0;
 6     y = x + 1;
 7     z = x - 1;
 8     r = y - z;
 9     __ASTREE_log_vars((r));
10 }
% gcc double-error.c
% ./a.out
134217728.000000
% astree -exec-fn main -print-float-digits 10 double-error.c |& grep "r in
direct = <float-interval: r in [-134217728, 134217728] >
12 ASTRÉE makes a worst-case assumption on the rounding (+∞, -∞, 0, nearest) hence the possibility to get -134217728.
```

Example of accumulation of small rounding errors

```
% cat -n rounding-c.c
 1 #include <stdio.h>
 2 int main () {
 3     int i; double x; x = 0.0;
 4     for (i=1; i<=10000000000; i++) {
 5         x = x + 1.0/10.0;
 6     }
 7     printf("x = %f\n", x);
 8 }
% gcc rounding-c.c
% ./a.out
x = 99999998.745418
%
```

$$\text{since } (0.1)_{10} = (0.0001100110011001100\dots)_2$$



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The Patriot missile failure

- “On February 25th, 1991, a Patriot missile ... failed to track and intercept an incoming Scud ^(*).”
- The **software failure** was due to accumulated rounding error ^(†)

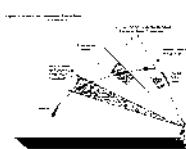


^(*) This Scud subsequently hit an Army barracks, killing 28 Americans.

^(†) – “Time is kept continuously by the system’s internal clock in tenths of seconds”

– “The system had been in operation for over 100 consecutive hours”

– “Because the system had been on so long, the resulting inaccuracy in the time calculation caused the range gate to shift so much that the system could not track the incoming Scud”



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Static analysis with ASTRÉE

```
% cat -n rounding.c
 1 int main () {
 2     double x; x = 0.0;
 3     while (1) {
 4         x = x + 1.0/10.0;
 5         __ASTREE_log_vars((x));
 6         __ASTREE_wait_for_clock();
 7     }
 8 }
% cat rounding.config
__ASTREE_max_clock((1000000000));
% astree -exec-fn main -config-sem rounding.config -unroll 0 rounding.c \
|& egrep "(x in) |(\|x\|) |(WARN)" | tail -2
direct = <float-interval: x in [0.1, 200000040.938] >
|x| <= 1.*((0. + 0.1/(1.-1))*(1.)^clock - 0.1/(1.-1)) + 0.1
<= 200000040.938
```



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Scaling



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Static Analysis of Scaling with ASTRÉE

```
% cat -n scale.c           % gcc scale.c
 1 int main () {          % ./a.out
 2   float x; x = 0.70000001;    x = 0.69999998079071
 3   while (1) {
 4     x = x / 3.0;
 5     x = x * 3.0;
 6     __ASTREE_log_vars((x));
 7     __ASTREE_wait_for_clock();
 8   }
 9 }
```

```
% cat scale.config
__ASTREE_max_clock((1000000000));
% astree -exec-fn main -config-sem scale.config -unroll 0 scale.c \
|& grep "x in" | tail -1
direct = <float-interval: x in [0.69999986887, 0.700000047684] >
```

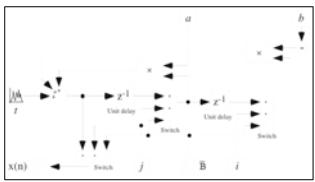




Filtering

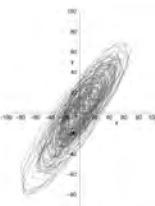


2^d Order Digital Filter:

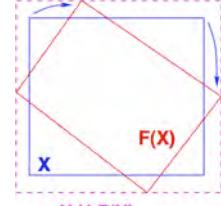


Ellipsoid Abstract Domain for Filters

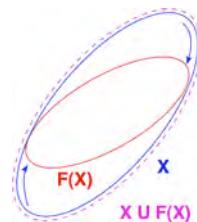
- Computes $X_n = \begin{cases} \alpha X_{n-1} + \beta X_{n-2} + Y_n \\ I_n \end{cases}$
- The concrete computation is bounded, which must be proved in the abstract.
- There is no stable interval or octagon.
- The simplest stable surface is an ellipsoid.



execution trace



unstable interval



stable ellipsoid



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Filter Example [Fer04]

```
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
BOOLEAN INIT; float P, X;
void filter () {
  static float E[2], S[2];
  if (INIT) { S[0] = X; P = X; E[0] = X; }
  else { P = (((((0.5 * X) - (E[0] * 0.7)) + (E[1] * 0.4))
               + (S[0] * 1.5)) - (S[1] * 0.7)); }
  E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;
  /* S[0], S[1] in [-1327.02698354, 1327.02698354] */
}
void main () { X = 0.2 * X + 5; INIT = TRUE;
  while (1) {
    X = 0.9 * X + 35; /* simulated filter input */
    filter (); INIT = FALSE; }
}
```



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Time Dependence



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```
% cat count.c
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
volatile BOOLEAN I; int R; BOOLEAN T;
void main() {
    R = 0;
    while (TRUE) {
        _ASTREE_log_vars((R));
        if (I) { R = R + 1; }           ← potential overflow!
        else { R = 0; }
        T = (R >= 100);
        _ASTREE_wait_for_clock();
    }
}

% cat count.config
_ ASTREE_volatile_input((I [0,1]));
_ ASTREE_max_clock((3600000));
% astree -exec-fn main -config-sem count.config count.c|grep '|R|'
|R| <= 0. + clock *1. <= 3600001.
```



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Arithmetic-Geometric Progressions (Example 1)



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Arithmetic-Geometric Progressions: Example 2

```
% cat retro.c
typedef enum {FALSE=0, TRUE=1} BOOL;
BOOL FIRST;
volatile BOOL SWITCH;
volatile float E;
float P, X, A, B;

void dev( )
{ X=E;
  if (FIRST) { P = X; }
  else
    { P = (P - (((2.0 * P) - A) - B)
           * 4.491048e-03)); }
  B = A;
  if (SWITCH) {A = P;}
  else {A = X;}
}

void main()
{ FIRST = TRUE;
  while (TRUE) {
    dev();
    FIRST = FALSE;
    _ASTREE_wait_for_clock();
  }
}

% cat retro.config
_ ASTREE_volatile_input((E [-15.0, 15.0]));
_ ASTREE_volatile_input((SWITCH [0,1]));
_ ASTREE_max_clock((3600000));
|P| <= (15. + 5.87747175411e-39
/ 1.19209290217e-07) * (1
+ 1.19209290217e-07)^clock
- 5.87747175411e-39 /
1.19209290217e-07 <= 23.0393526881
```

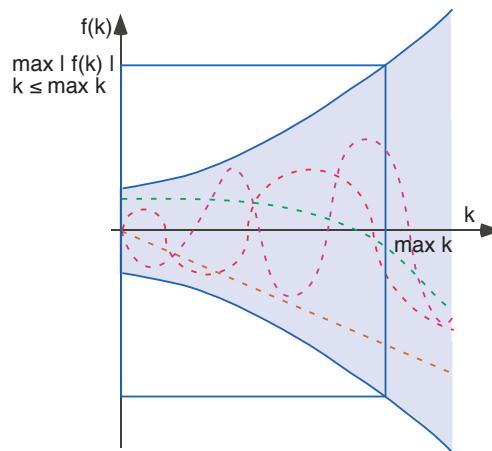


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Overapproximation with an Arithmetic-Geometric Progression



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Arithmetic-geometric progressions¹³ [Fer05]

– Abstract domain: $(\mathbb{R}^+)^5$

– Concretization:

$$\gamma \in (\mathbb{R}^+)^5 \mapsto \wp(\mathbb{N} \mapsto \mathbb{R})$$

$$\gamma(M, a, b, a', b') =$$

$$\{f \mid \forall k \in \mathbb{N} : |f(k)| \leq (\lambda x \cdot ax + b \circ (\lambda x \cdot a'x + b')^k)(M)\}$$

i.e. any function bounded by the arithmetic-geometric progression.

¹³ here in \mathbb{R}



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Reference

- [1] J. Feret. The arithmetic-geometric progression abstract domain. In VMCAI'05, Paris, LNCS 3385, pp. 42–58, Springer, 2005.

4. The industrial use of ASTRÉE



References

- [2] D. Delmas and J. Souyris. ASTRÉE: from Research to Industry. Proc. 14th Int. Symp. SAS '07, G. Filé and H. Riis-Nielson (eds), 22–24 Aug. 2007, Kongens Lyngby, DK, LNCS 4634, pp. 437–451, Springer.



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Digital Fly-by-Wire Avionics¹⁴



¹⁴ The electrical flight control system is placed between the pilot's controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement they control and monitor.

Example application

- Primary flight control software of the Airbus A340 family/A380 fly-by-wire system



- C program, automatically generated from a proprietary high-level specification (à la Simulink/SCADE)
- A340 family: 132,000 lines, 75,000 LOCs after preprocessing, 10,000 global variables, over 21,000 after expansion of small arrays, now × 2

A380: × 3/7

Benchmarks (Airbus A340 Primary Flight Control Software)

- V1¹⁵, 132,000 lines, 75,000 LOCs after preprocessing
- Comparative results (commercial software):
4,200 (false?) alarms, 3.5 days;
- Our results:
0 alarms,
40mn on 2.8 GHz PC, 300 Megabytes
→ A world première in Nov. 2003!

¹⁵ "Flight Control and Guidance Unit" (FCGU) running on the "Flight Control Primary Computers" (FCPC). The three primary computers (FCPC) and two secondary computers (FCS2) which form the A340 and A330 electrical flight control system are placed between the pilot's controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement they control and monitor.

The main loop invariant for the A340 V1

A textual file over 4.5 Mb with

- 6,900 boolean interval assertions ($x \in [0; 1]$)
- 9,600 interval assertions ($x \in [a; b]$)
- 25,400 clock assertions ($x + \text{clk} \in [a; b] \wedge x - \text{clk} \in [a; b]$)
- 19,100 additive octagonal assertions ($a \leq x + y \leq b$)
- 19,200 subtractive octagonal assertions ($a \leq x - y \leq b$)
- 100 decision trees
- 60 ellipse invariants, etc ...

involving over 16,000 floating point constants (only 550 appearing in the program text) \times 75,000 LOCs.



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Possible origins of imprecision and how to fix it

In case of false alarm, the imprecision can come from:

- **Abstract transformers** (not best possible) \longrightarrow improve algorithm;
- **Automatized parametrization** (e.g. variable packing) \longrightarrow improve pattern-matched program schemata;
- **Iteration strategy** for fixpoints \longrightarrow fix widening¹⁶;
- **Inexpressivity** i.e. indispensable local inductive invariant are inexpressible in the abstract \longrightarrow add a **new abstract domain** to the reduced product (e.g. filters).

¹⁶ This can be very hard since at the limit only a precise infinite iteration might be able to compute the proper abstract invariant. In that case, it might be better to design a more refined abstract domain.



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(Airbus A380 Primary Flight Control Software)

- 0 alarms (Nov. 2004), after some additional parametrization and simple abstract domains developments
- Now at 1,000,000 lines!

34h,

8 Gigabyte

\longrightarrow A world grand première!



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5. Conclusion



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Characteristics of the ASTRÉE Analyzer

- Sound:** – ASTRÉE is a **bug eradicator**: finds all bugs in a well-defined class (runtime errors)
- ASTRÉE is not a **bug hunter**: finding some bugs in a well-defined class (e.g. by *bug pattern detection* like FindBugs™, PREfast or PMD)
- ASTRÉE is **exhaustive**: covers the whole state space (\neq MAGIC, CBMC)
- ASTRÉE is **comprehensive**: never omits potential errors (\neq UNO, CMC from coverity.com) or sort most probable ones to avoid overwhelming messages (\neq Splint)



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Characteristics of the ASTRÉE Analyzer (Cont'd)

Multiabstraction: uses many numerical/symbolic abstract domains (\neq symbolic constraints in Bane or the canonical abstraction of TVLA)

Infinitary: all abstractions use infinite abstract domains with widening/narrowing (\neq model checking based analyzers such as Bandera, Bogor, Java PathFinder, Spin, VeriSoft)

Efficient: always terminate (\neq counterexample-driven automatic abstraction refinement BLAST, SLAM)



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Characteristics of the ASTRÉE Analyzer (Cont'd)

Static: compile time analysis (\neq run time analysis Rational Purify, Parasoft Insure++)

Program Analyzer: analyzes programs not micromodels of programs (\neq PROMELA in SPIN or Alloy in the Alloy Analyzer)

Automatic: no end-user intervention needed (\neq ESC Java, ESC Java 2), or PREfast (annotate functions with intended use)



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Characteristics of the ASTRÉE Analyzer (Cont'd)

Extensible/Specializable: can easily incorporate new abstractions (and reduction with already existing abstract domains) (\neq general-purpose analyzers PolySpace Verifier)

Domain-Aware: knows about control/command (e.g. digital filters) (as opposed to specialization to a mere programming style in C Global Surveyor)

Parametric: the precision/cost can be tailored to user needs by options and directives in the code



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Characteristics of the ASTRÉE Analyzer (Cont'd)

Automatic Parametrization: the generation of parametric directives in the code can be programmed (to be specialized for a specific application domain)

Modular: an analyzer instance is built by selection of OCAML modules from a collection each implementing an abstract domain

Precise: very few or no false alarm when adapted to an application domain → it is a **VERIFIER!**



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THE END



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The Future of the ASTRÉE Analyzer

- ASTRÉE has shown **usable** and **useful** in one industrial context (*electric flight control*):
 - as a R & D tool for A340 V2 and A380;
 - as a production tool for the A350;
- **More applications** are forthcoming (ES_PASS project);
- **Industrialization** is simultaneously under consideration.



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THE END, THANK YOU



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6. Bibliography



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◀◀◀◀- ? | ▶▶▶▶ ▷

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- [CC77] P. Cousot and R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In *Conference Record of the Fourth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 238–252, Los Angeles, Californie, 1977. ACM Press, New York, New York, USA.
- [CC79] P. Cousot and R. Cousot. Systematic design of program analysis frameworks. In *Conference Record of the Sixth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 269–282, San Antonio, Texas, 1979. ACM Press, New York, New York, USA.
- [CC92a] P. Cousot and R. Cousot. Abstract interpretation frameworks. *Journal of Logic and Computation*, 2(4):511–547, août 1992.
- [CC92b] P. Cousot and R. Cousot. Inductive definitions, semantics and abstract interpretation. In *Conference Record of the Ninteenth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 83–94, Albuquerque, Nouveau Mexique, USA, 1992. ACM Press, New York, New York, USA.
- [CC95] P. Cousot and R. Cousot. Formal language, grammar and set-constraint-based program analysis by abstract interpretation. In *Proceedings of the Seventh ACM Conference on Functional Programming Languages and Computer Architecture*, pages 170–181, La Jolla, Californie, USA, 25–28 juin 1995. ACM Press, New York, New York, USA.
- [CC00] P. Cousot and R. Cousot. Temporal abstract interpretation. In *Conference Record of the Twentyseventh Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 12–25, Boston, Massachusetts, USA, janvier 2000. ACM Press, New York, New York, USA.



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[AGM93] G. Amato, F. Giannotti, and G. Mainetto. Data sharing analysis for a database programming language via abstract interpretation. In R. Agrawal, S. Baker, and D.A.Bell, editors, *Proceedings of the Nineteenth International Conference on Very Large Data Bases*, pages 405–415, Dublin, Irlande, 24–27 août 1993. MORGANKAUFMANN.

[BCC⁺02] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. Design and implementation of a special-purpose static program analyzer for safety-critical real-time embedded software, chapitre invit . In T. Mogensen, D.A. Schmidt, and I.H. Sudborough, editors, *The Essence of Computation: Complexity, Analysis, Transformation. Essays Dedicated to Neil D. Jones*, Lecture Notes in Computer Science 2566, pages 85–108. Springer, Berlin, Allemagne, 2002.

[BCC⁺03] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Min , D. Monniaux, and X. Rival. A static analyzer for large safety-critical software. In *Proceedings of the ACM SIGPLAN'2003 Conference on Programming Language Design and Implementation (PLDI)*, pages 196–207, San Diego, Californie, USA, 7–14 juin 2003. ACM Press, New York, New York, USA.

[BPC01] J. Bailey, A. Poulovassilis, and C. Courtenage. Optimising active database rules by partial evaluation and abstract interpretation. In *Proceedings of the Eight International Workshop on Database Programming Languages*, Lecture Notes in Computer Science 2397, pages 300–317, Frascati, Italie, 8–10 septembre 2001. Springer, Berlin, Allemagne.

[BS97] V. Benzaken and X. Schaefer. Static integrity constraint management in object-oriented database programming languages via predicate transformers. In M. Aksit and S. Matsuoka, editors, *Proceedings of the Eleventh European Conference on Object-Oriented Programming, ECOOP'97*, Lecture Notes in Computer Science 1241. Springer, Berlin, Allemagne, Jyv skyl , Finlande, 9–13 juin 1997.

Seminar, Colloquia Patavina, Padova, 19/2/2008 ◀◀◀◀- ? | ▶▶▶▶ ▷ © P. Cousot

[CC02] P. Cousot and R. Cousot. Systematic design of program transformation frameworks by abstract interpretation. In *Conference Record of the Twentyninth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 178–190, Portland, Oregon, USA, janvier 2002. ACM Press, New York, New York, USA.

[CC03] P. Cousot and R. Cousot. Parsing as abstract interpretation of grammar semantics. *Theoretical Computer Science*, 290(1):531–544, janvier 2003.

[CC04] P. Cousot and R. Cousot. An abstract interpretation-based framework for software watermarking. In *Conference Record of the Thirtyfirst Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 173–185, Venise, Italie, 14–16 janvier 2004. ACM Press, New York, New York, USA.

[CCF⁺05] P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Min , D. Monniaux, and X. Rival. The ASTR  analyser. In M. Sagiv, editor, *Proceedings of the Fourteenth European Symposium on Programming Languages and Systems, ESOP'2005*,  dimbourg,  cosse, volume 3444 of *Lecture Notes in Computer Science*, pages 21–30. Springer, Berlin, Allemagne, 2–10 avril 2005.

[CCF⁺07] P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Min , D. Monniaux, and X. Rival. Varieties of static analyzers: A comparison with ASTR , papier invit . In M. Hinckey, He Jifeng, and J. Sanders, editors, *Proceedings of the First IEEE & IFIP International Symposium on Theoretical Aspects of Software Engineering, TASE'07*, pages 3–17, Shanghai, Chine, 6–8 juin 2007. IEEE Computer Society Press, Los Alamitos, Californie, USA.

Seminar, Colloquia Patavina, Padova, 19/2/2008 ◀◀◀◀- ? | ▶▶▶▶ ▷ © P. Cousot

- [CCF⁺08] P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. Combination of abstractions in the ASTRÉE static analyzer, papier invit . In M. Okada and I. Satoh, editors, *Eleventh Annual Asian Computing Science Conference, ASIAN'06*, Tokyo, Japon, 6-8 d cembre 2006, 2008. Lecture Notes in Computer Science 4435, Springer, Berlin, Allemagne.
- [CH78] P. Cousot and N. Halbwachs. Automatic discovery of linear restraints among variables of a program. In *Conference Record of the Fifth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 84-97, Tucson, Arizona, 1978. ACM Press, New York, New York, USA.
- [Cou78] P. Cousot. *M thodes it ratives de construction et d'approximation de points fixes d'op ateurs monotones sur un treillis, analyse s mantique de programmes*. Th se d' tat  s sciences math matiques, Universit  scientifique et m dicale de Grenoble, Grenoble, 21 mars 1978.
- [Cou81] P. Cousot. Semantic foundations of program analysis, chapitre invit . In S.S. Muchnick and N.D. Jones, editors, *Program Flow Analysis: Theory and Applications*, chapter 10, pages 303-342. Prentice-Hall, Inc., Englewood Cliffs, New Jersey, USA, 1981.
- [Cou97] P. Cousot. Types as abstract interpretations, papier invit . In *Conference Record of the Twenty-fourth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 316-331, Paris, janvier 1997. ACM Press, New York, New York, USA.
- [Cou02] P. Cousot. Constructive design of a hierarchy of semantics of a transition system by abstract interpretation. *Theoretical Computer Science*, 277(1-2):47-103, 2002.

- [FHL⁺01] C. Ferdinand, R. Heckmann, M. Langenbach, F. Martin, M. Schmidt, H. Theiling, S. Thesing, and R. Wilhelm. Reliable and precise WCET determination for a real-life processor. In T.A. Henzinger and C.M. Kirsch, editors, *Proceedings of the First International Workshop on Embedded Software, EMSOFT'2001*, volume 2211 of *Lecture Notes in Computer Science*, pages 469-485. Springer, Berlin, Allemagne, 2001.
- [GM04] R. Giacobazzi and I. Mastroeni. Abstract non-interference: Parameterizing non-interference by abstract interpretation. In *Conference Record of the Thirtyfirst Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 186-197, Venise, Italie, 2004. ACM Press, New York, New York, USA.
- [JP06] Ph. Jorrand and S. Perdrix. Towards a quantum calculus. In *Proceedings of the Fourth International Workshop on Quantum Programming Languages*, ENTCS, 2006.
- [Mau04] L. Mauborgne. ASTR E: Verification of absence of run-time error. In P. Jacquot, editor, *Building the Information Society*, chapter 4, pages 385-392. Kluwer Academic Publishers, Dordrecht, Pays-Bas, 2004.
- [Min] A. Min . The Octagon abstract domain library. <http://www.di.ens.fr/~mine/oct/>.
- [Min04a] A. Min . Relational abstract domains for the detection of floating-point run-time errors. In D. Schmidt, editor, *Proceedings of the Thirteenth European Symposium on Programming Languages and Systems, ESOP'2004*, Barcelone, Espagne, volume 2986 of *Lecture Notes in Computer Science*, pages 3-17. Springer, Berlin, Allemagne, mars 27 - avril 4, 2004.
- [Min04b] A. Min . *Weakly Relational Numerical Abstract Domains*. Th se de doctorat en informatique,  cole polytechnique, Palaiseau, 6 d cembre 2004.

- [Cou03] P. Cousot. Verification by abstract interpretation, chapitre invit . In N. Dershowitz, editor, *Proceedings of the International Symposium on Verification - Theory & Practice - Honoring Zohar Manna's 64th Birthday*, pages 243-268. Lecture Notes in Computer Science 2772, Springer, Berlin, Allemagne, Taormina, Italie, 29 juin - 4 juillet 2003.
- [Cou07] P. Cousot. Proving the absence of run-time errors in safety-critical avionics code, expos  invit . In *Proceedings of the Seventh ACM & IEEE International Conference on Embedded Software, EMSOFT'2007*, pages 7-9. ACM Press, New York, New York, USA, 2007.
- [Dan07] V. Danos. Abstract views on biological signaling. In *Mathematical Foundations of Programming Semantics, Twentythird Annual Conference (MFPS XXIII)*, 2007.
- [DS07] D. Delmas and J. Souyris. ASTR E: from research to industry. In G. Fil  and H. Riis-Nielson, editors, *Proceedings of the Fourteenth International Symposium on Static Analysis, SAS'07*, Kongens Lyngby, Danemark, Lecture Notes in Computer Science 4634, pages 437-451. Springer, Berlin, Allemagne, 22-24 ao t 2007.
- [Fer04] J. Feret. Static analysis of digital filters. In D. Schmidt, editor, *Proceedings of the Thirteenth European Symposium on Programming Languages and Systems, ESOP'2004*, Barcelone, Espagne, volume 2986 of *Lecture Notes in Computer Science*, pages 33-48. Springer, Berlin, Allemagne, mars 27 - avril 4, 2004.
- [Fer05] J. Feret. The arithmetic-geometric progression abstract domain. In R. Cousot, editor, *Proceedings of the Sixth International Conference on Verification, Model Checking and Abstract Interpretation (VMCAI 2005)*, pages 42-58, Paris, 17-19 janvier 2005. Lecture Notes in Computer Science 3385, Springer, Berlin, Allemagne.

- [Min05] A. Min . Weakly relational numerical abstract domains: Theory and application, papier invit . In *First International Workshop on Numerical & Symbolic Abstract Domains, NSAD'05*, Maison Des Polytechniciens, Paris, 21 janvier 2005.
- [Min06a] A. Min . Field-sensitive value analysis of embedded C programs with union types and pointer arithmetics. In *Proceedings of the ACM SIGPLAN/SIGBED Conference on Languages, Compilers, and Tools for Embedded Systems, LCTES'2006*, pages 54-63. ACM Press, New York, New York, USA, juin 2006.
- [Min06b] A. Min . The octagon abstract domain. *Higher-Order and Symbolic Computation*, 19:31-100, 2006.
- [Min06c] A. Min . Symbolic methods to enhance the precision of numerical abstract domains. In E.A. Emerson and K.S. Namjoshi, editors, *Proceedings of the Seventh International Conference on Verification, Model Checking and Abstract Interpretation (VMCAI 2006)*, pages 348-363, Charleston, Caroline du Sud, USA, 8-10, janvier 2006. Lecture Notes in Computer Science 3855, Springer, Berlin, Allemagne.
- [Mon05] D. Monniaux. The parallel implementation of the ASTR E static analyzer. In *Proceedings of the Third Asian Symposium on Programming Languages and Systems, APLAS'2005*, pages 86-96, Tsukuba, Japon, 3-5 novembre 2005. Lecture Notes in Computer Science 3780, Springer, Berlin, Allemagne.
- [MR05] L. Mauborgne and X. Rival. Trace partitioning in abstract interpretation based static analyzer. In M. Sagiv, editor, *Proceedings of the Fourteenth European Symposium on Programming Languages and Systems, ESOP'2005*,  Edimbourg, Ecossie, volume 3444 of *Lecture Notes in Computer Science*, pages 5-20. Springer, Berlin, Allemagne, avril 2-10, 2005.

- [PCJD07] M. Dalla Preda, M. Christodorescu, S. Jha, and S. Debray. Semantics-based approach to malware detection. In *Conference Record of the Thirtyfourth Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, pages 238–252, Nice, France, 17–19 janvier 2007. ACM Press, New York, New York, USA.
- [Per06] S. Perdrix. *Modèles formels du calcul quantique : ressources, machines abstraites et calcul par mesure*. PhD thesis, Institut National Polytechnique de Grenoble, Laboratoire Leibniz, 2006.
- [Riv05a] X. Rival. Abstract dependences for alarm diagnosis. In *Proceedings of the Third Asian Symposium on Programming Languages and Systems, APLAS'2005*, pages 347–363, Tsukuba, Japon, 3–5 novembre 2005. Lecture Notes in Computer Science 3780, Springer, Berlin, Allemagne.
- [Riv05b] X. Rival. Understanding the origin of alarms in ASTRÉE. In C. Hankin and I. Siveroni, editors, *Proceedings of the Twelfth International Symposium on Static Analysis, SAS '05*, pages 303–319, Londres, Royaume Uni, Lecture Notes in Computer Science 3672, 7–9 septembre 2005.
- [RT04] F. Ranzato and F. Tapparo. Strong preservation as completeness in abstract interpretation. In D. Schmidt, editor, *Proceedings of the Thirteenth European Symposium on Programming Languages and Systems, ESOP '04*, volume 2986 of *Lecture Notes in Computer Science*, pages 18–32, Barcelone, Espagne, mars 29 – avril 2 2004. Springer, Berlin, Allemagne.
- [RT06] F. Ranzato and F. Tapparo. Strong preservation of temporal fixpoint-based operators by abstract interpretation. In A.E. Emerson and K.S. Namjoshi, editors, *Proceedings of the Seventh International Conference on Verification, Model Checking and Abstract Interpretation (VMCAI 2006)*, pages 332–347, Charleston, Caroline du Sud, USA, 8–10 janvier 2006. Lecture Notes in Computer Science 3855 , Springer, Berlin, Allemagne.



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