« Avionic Software Verification by Abstract Interpretation »

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Abstract

A flight control surface actuation system in avionics is safety critical and complex since it is placed between the pilot's controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement it controls and monitors. For reliability and dependability, several redundant software and computers are used but each one must be proved to be correct. With the exponential increase of the power of computers, the flight control software has become much more powerful hence complex. Since the cost of tests increasing more rapidly that the size of programs, formal methods become an attractive complement for program verification.

The difficulties with formal methods are that they need a formal specification, a formal semantics of the programming language and, because of undecidability, have serious limits in the automatic verification that the program semantics satisfies the specification. A theorem prover needs human assistance while model-checking requires finite models which, but for hardware, are generally incomplete.

Static analysis offers an interesting completely automatic alternative in that the specification can be chosen to be implicit. For example the absence of runtime error will not require the user to define a complex specification. Moreover static analysis considers infinite models of computations that can be directly computed from the program text so that the end-user does not need to provide a (finite) model of the program computations and environment. Finally, the reachable states during any program computation are computed approximately through an overapproximation that omits no possible case. So the delicate questions about the program semantics can be solved by considering all possible alternatives.

If this overapproximation copes with the undecidability problem, its inconvenience is that it considers spurious program behaviors, which do not exist in any actual execution, but may be at the origin of alarms, so-called false alarms". This approach is sound in that no runtime error will ever be omitted in the diagnostic. It is incomplete, because of the potential false alarms. In general false alarms have to be solved by manual code inspection, which is extremely costly.





The whole problem is therefore to choose abstractions of the program semantics that yield few or no alarm. To do so, one can restrict the family of programs to be analyzed so as to adapt the abstraction exactly the domain-specific primitives and algorithmic schema found in this family of programs.

We will present elements of the theory of abstract interpretation on which the soundness of the notion of overapproximation does rely. Then we will introduce the ASTRÉE static analyzer (www.astree.ens.fr), which is specialized for the verification of the absence of runtime errors in control-command programs. The analyzer has general-purpose abstractions (e.g. octagons, control and data partitioning) as well as domain-specific abstractions (e.g. to handle filters or the potential accumulation of rounding errors). Finally, we will report on the successful application of ASTRÉE to the proof of absence of runtime errors in recent avionic flight control software.



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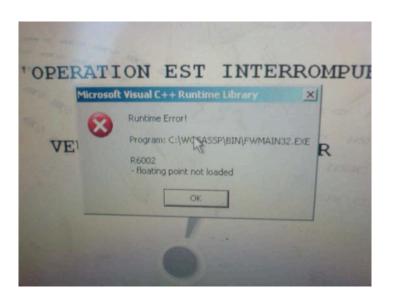
Motivation



Bugs Now Show-Up in Everyday Life

- Bugs now appear frequently in everyday life (banks, cars, telephones, ...)
- Example (HSBC bank ATM¹ at 19 Boulevard Sébastopol in Paris, failure on Nov. 21st 2006 at 8:30 am):





¹ cash machine, cash dispenser, automatic teller machine.





A Strong Need for Software Better Quality

 Poor software quality is not acceptable in safety and mission critical software applications.









- The present state of the art in software engineering does not offer sufficient quality garantees



The Complexity of Software Design

- The design of complex software is difficult and economically critical
- Example (www.designnews.com/article/CA6475332.html): Boeing Confirms 787 Delay, Fasteners, Flight Control Software Code Blamed John Dodge, Editor-in-Chief – Design News, September 5, 2007

Boeing officials confirmed today that a fastener shortage and problems with flight control software have pushed "first flight" of the Boeing 787 Dreamliner to sometime between mid-November and mid-December.

The software delays involve Honeywell Aerospace, which is responsible for flight control software. The work on this part of the 787 was simply underestimated, said Bair.



Tool-Based Software Design Methods

- New tool-based software design methods will have to emerge to face the unprecedented growth and complexification of critical software
- E.g. FCPC (Flight Control Primary Computer)
 - A220: 20 000 LOCs,
 - A340 (V1): 130 000 LOCS
 - A340 (V2): 250 000 LOCS
 - A380: 1.000.000 LOCS
 - A350: static analysis to be integrated in the software production







Static Analysis

A static analyzer is a program that

- takes as input:
 - a program P (written in some given programming language \mathbb{P} with a given semantics $\mathfrak{S}_{\mathbb{P}}$)
 - a specification S (implicit S[P] or written in some specification language \mathbb{S} with a given semantics $\mathfrak{S}_{\mathbb{S}}$)
- always terminates and delivers automatically as output:
 - a diagnosis on the validity of the program semantics with respect the specification semantics



Difficulties of Static Analysis

- automatic + infinite state + termination \Longrightarrow undecidable!
- for a programming (and a specification) language, not for a given model of a given program:

$$orall P \in \mathbb{P}: orall S \in \mathbb{S}: \mathfrak{S}_{\mathbb{P}}\llbracket P \rrbracket \subseteq \mathcal{S}_{\mathbb{S}}\llbracket P,S \rrbracket ?$$

or, more simply for an implicit specification $\mathfrak{S}||P||$:

$$orall P \in \mathbb{P}: \mathfrak{S}_{\mathbb{P}} \llbracket P \rrbracket \subseteq \mathfrak{S} \llbracket P \rrbracket?$$



Soundness and Completeness

- Soundness: for all $P \in \mathbb{P}$, if the answer is yes (no) then $\mathfrak{S}_{\mathbb{P}}[P] \subseteq \mathfrak{S}[P]$ (resp. $\mathfrak{S}_{\mathbb{P}}[P] \nsubseteq \mathfrak{S}[P]$)
- Completeness: for all $P \in \mathbb{P}$, if $\mathfrak{S}_{\mathbb{P}}[P] \subseteq \mathfrak{S}[P]$ ($\mathfrak{S}_{\mathbb{P}}[P] \nsubseteq \mathfrak{S}[P]$) then the answer is yes (resp. no)

We always require **Soundness!**

Undecidability \Longrightarrow no completeness



Problems with Formal Methods

- Formal specifications (abstract machines, temporal logic, ...) are costly, complex, error-prone, difficult to maintain, not mastered by casual programmers
- Formal semantics of the specification and programming language are inexistant, informal, irrealistic or complex
- Formal proofs are partial (static analysis), do not scale up (model checking) or need human assistance (theorem proving & proof assistants)
 - ⇒ High costs (for specification, proof assistance, etc).



Avantages of Static Analysis

- Formal specifications are implicit (no need for explicit, user-provided specifications)
- Formal semantics are approximated by the static analyzer (no user-provided models of the program)
- Formal proofs are automatic (no required user-interaction)
- Costs are low (no modification of the software production methodology)
- Scales up to 100.000 to 1.000.000 LOCS
- Rapid and large diffusion in embedded software production industries





Disadvantages of Static Analysis

- Imprecision (acceptable in some applications like WCET or program optimization)
- Incomplete for program verification
- False alarms are due to unsuccessful automatic proofs
 in 5 to 15% of the cases

For example, 1% of 500.000 potential (true or false) alarms is 5.000, too much to be handled by hand!



Remedies to False Alarms in Astrée

- Astrée is specialized to specific program properties 2
- ASTRÉE is specialized to real-time synchronous control/command programs written in C
- Astrée offers possibilities of refinement

The cost of adapting ASTRÉE to a specific program, should be a small fraction of the cost to test the specific program properties verified by ASTRÉE.

³ parametrizations and analysis directives





² proof of absence of runtime errors

Informal Introduction to Abstract Interpretation



Abstract Interpretation

There are two fundamental concepts in computer science (and in sciences in general) :

- Abstraction: to reason on complex systems
- Approximation: to make effective undecidable computations

These concepts are formalized by abstract interpretation

References

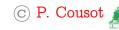
[POPL'77] P. Cousot and R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In 4th ACM POPL.

[Thesis '78] P. Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes. Thèse ès sci. math. Grenoble, march 1978.

[POPL'79] P. Cousot & R. Cousot. Systematic design of program analysis frameworks. In 6^{th} ACM POPL.







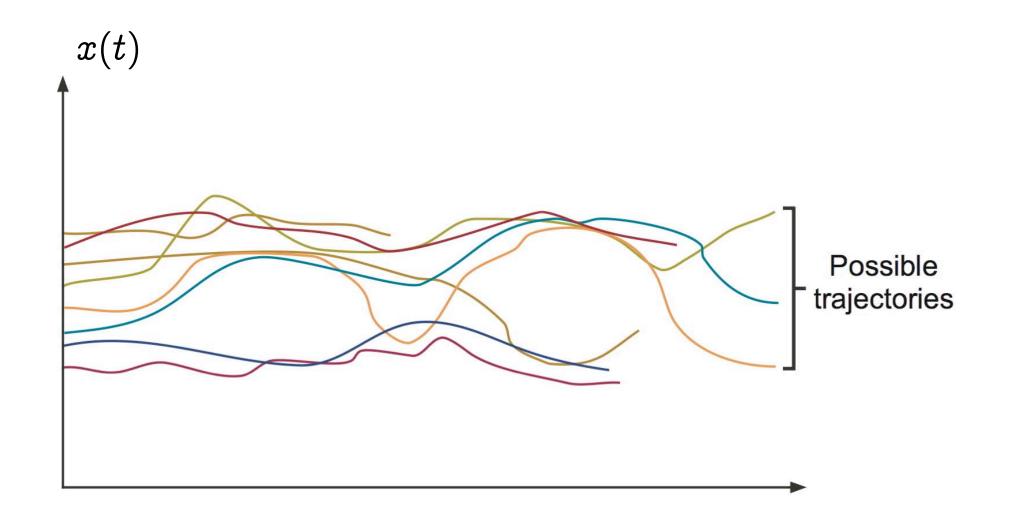


Principle of Abstraction





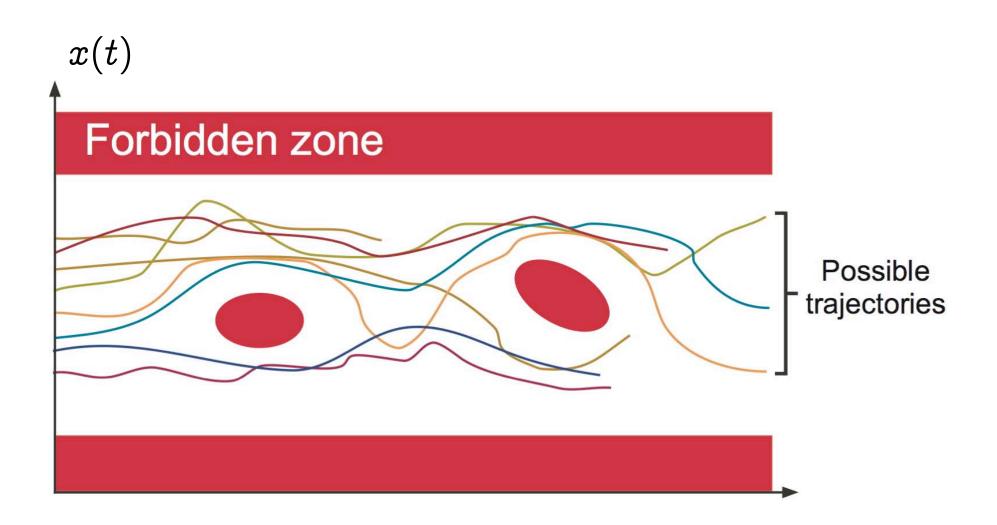
Operational semantics



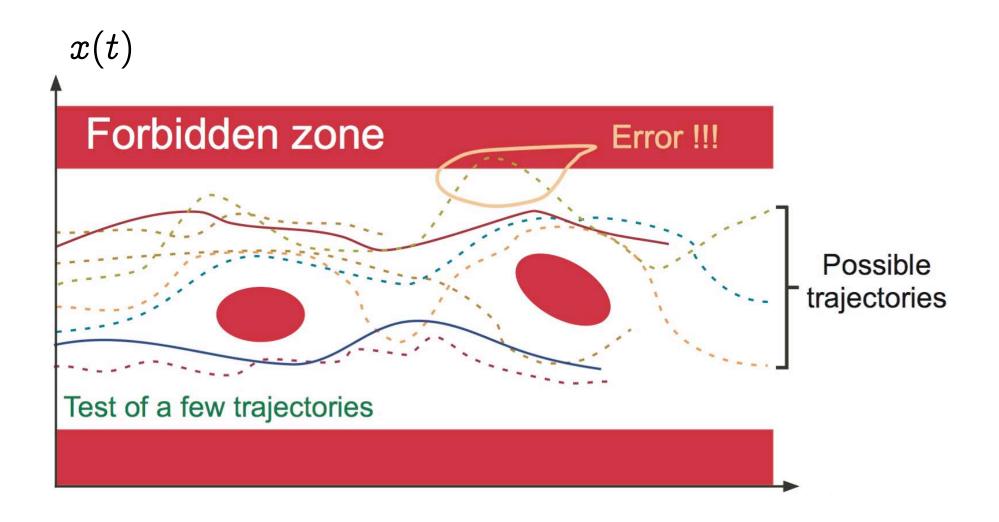




Safety property

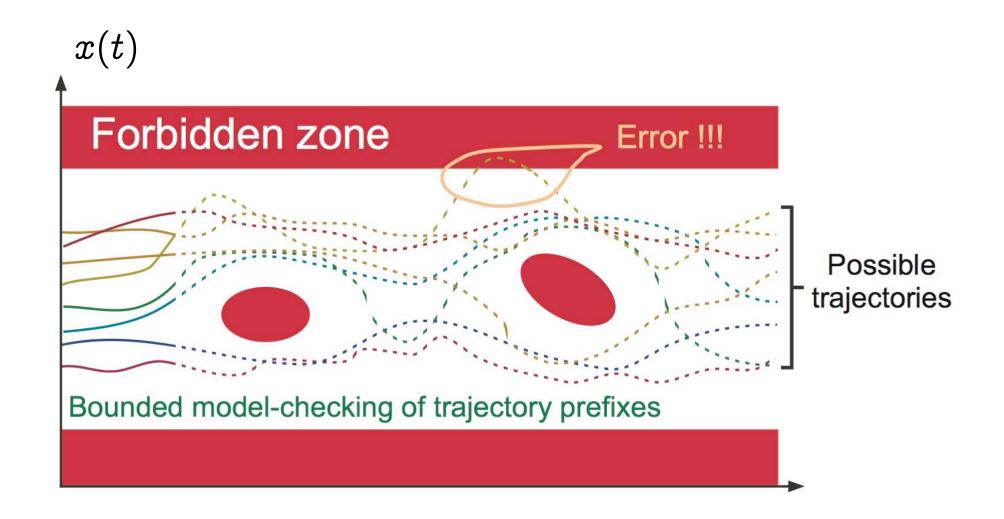


Test/Debugging is Unsafe

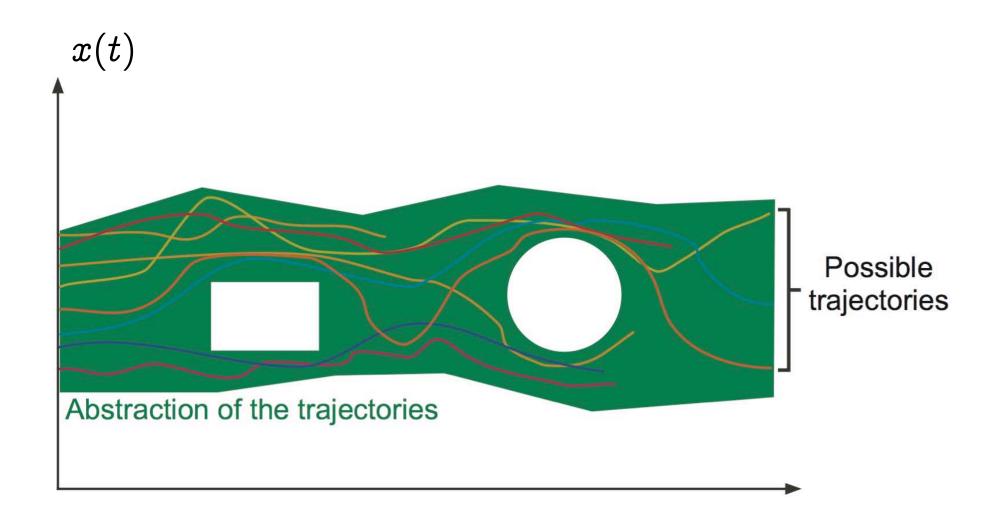




Bounded Model Checking is Unsafe



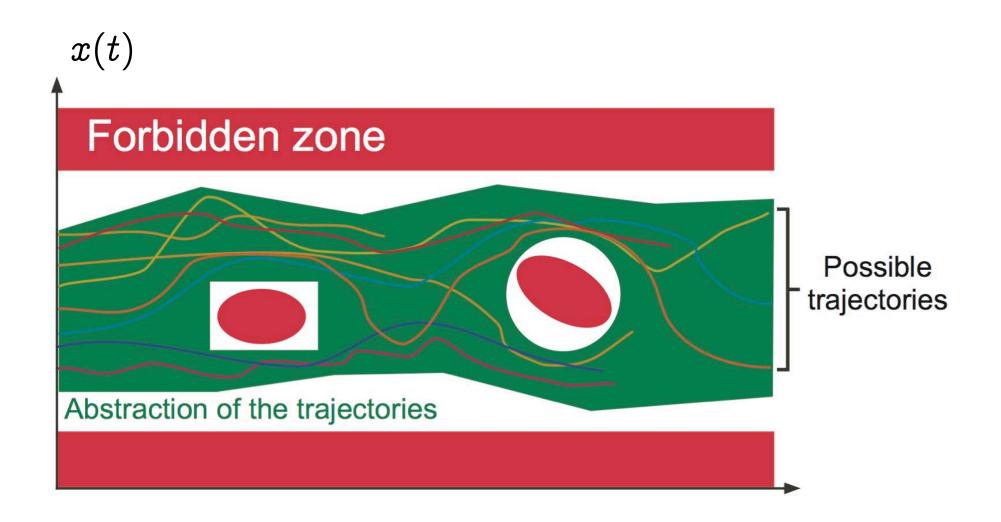
Over-Approximation







Abstract Interpretation is Sound





Soundness and Incompleteness





Soundness Requirement: Erroneous Abstraction ⁴

x(t)Forbidden zone Error !!! Possible trajectories Erroneous trajectory abstraction

⁴ This situation is <u>always excluded</u> in static analysis by abstract interpretation.









Soundness Requirement: Erroneous Abstraction ⁵

x(t)Forbidden zone Error !!! Possible trajectories Erroneous trajectory abstraction

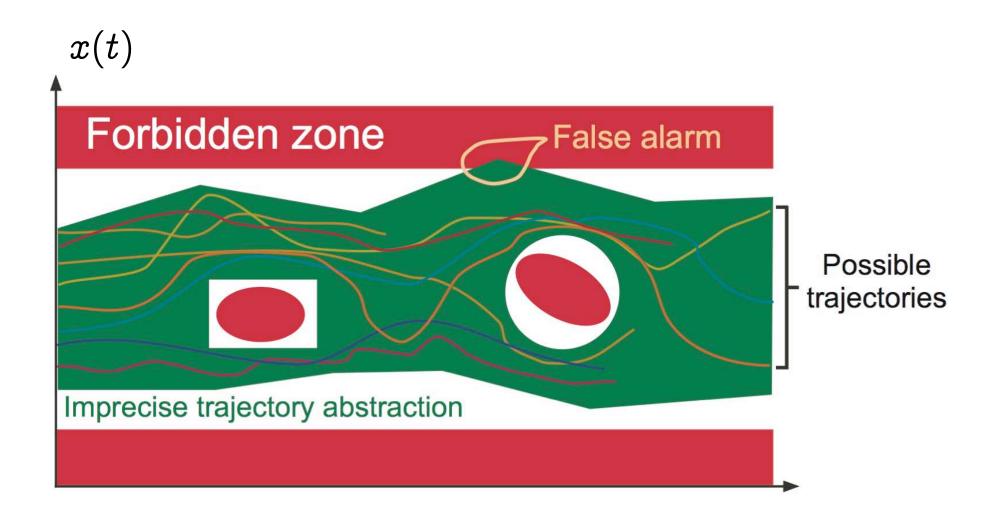
⁵ This situation is <u>always excluded</u> in static analysis by abstract interpretation.







Imprecision \Rightarrow False Alarms



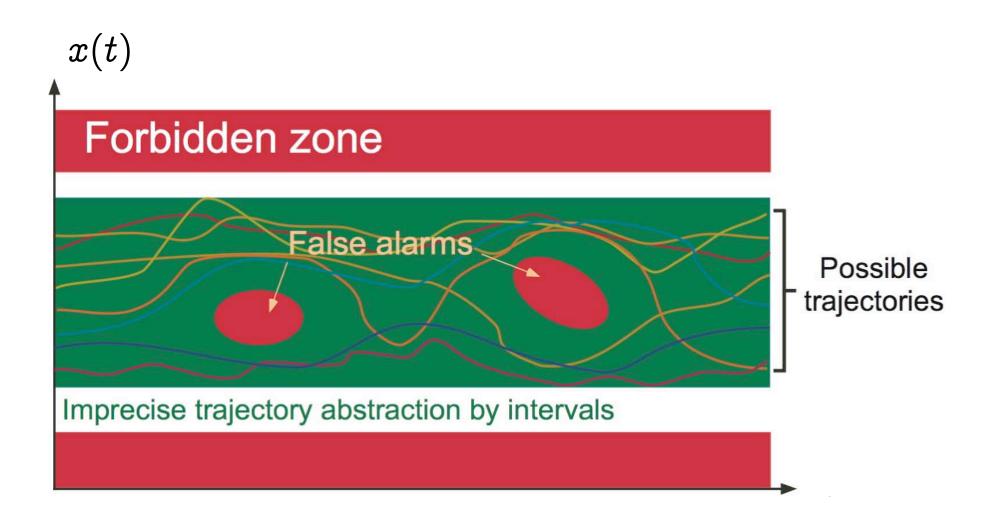




Design by Refinement

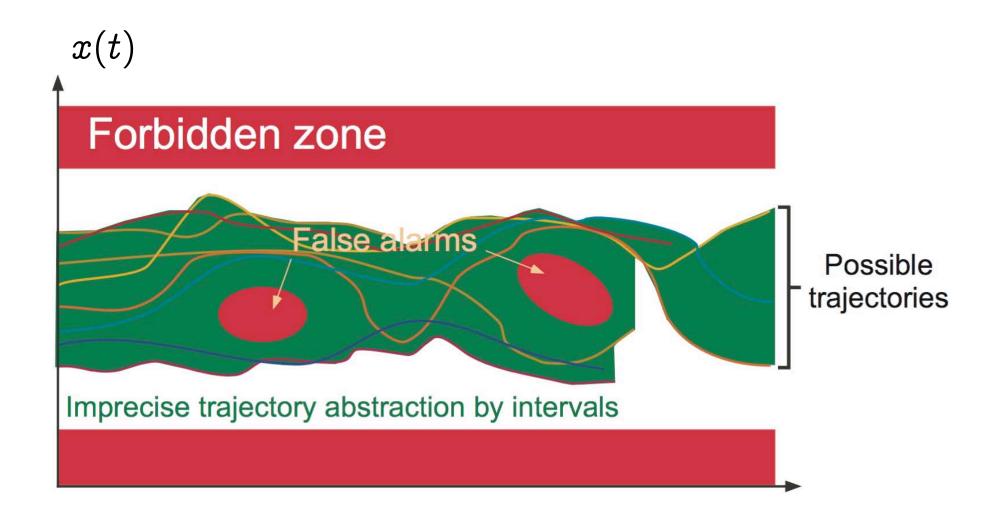


Global Interval Abstraction \rightarrow False Alarms



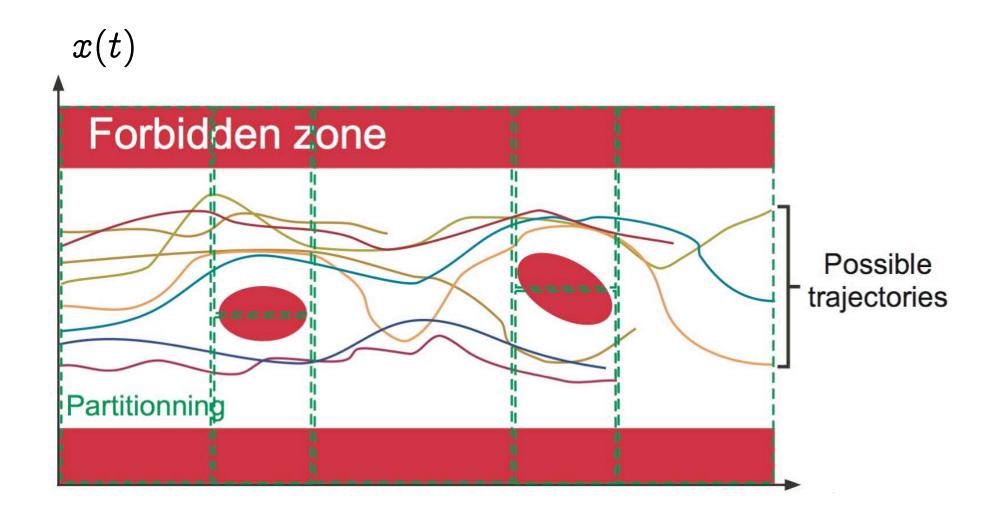


Local Interval Abstraction → False Alarms

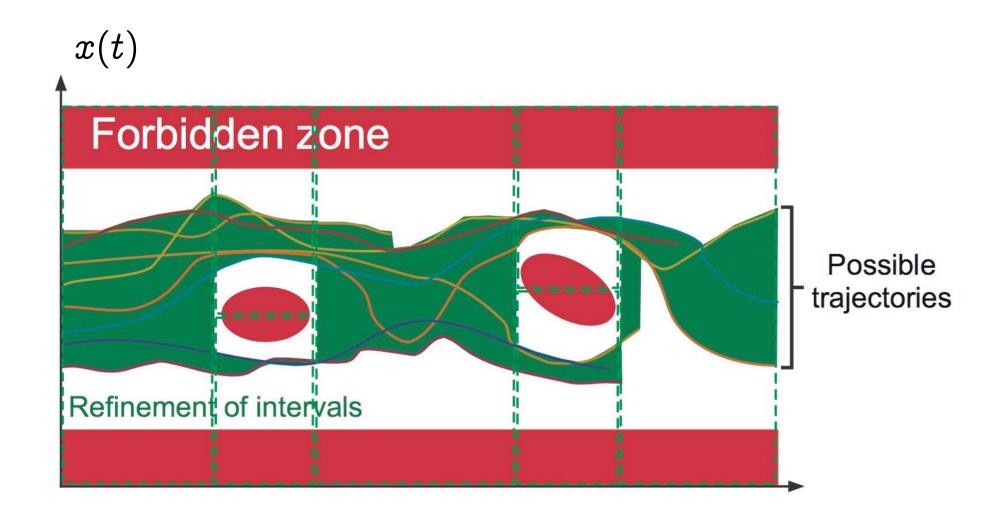




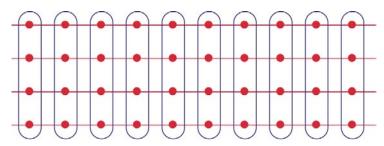
Refinement by Partitionning



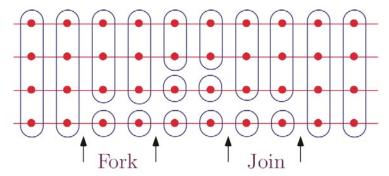
Intervals with Partitionning



State-based versus Trace-based Partitioning State-based partitionning at control points:



Trace-based partitionning at control points:



Delaying abstract unions in tests and loops is more precise for non-distributive abstract domains (and much less expensive than disjunctive completion).





Trace Partitioning

Principle:

- Semantic equivalence:

- More precise in the abstract: concrete execution paths are merged later.

Application:

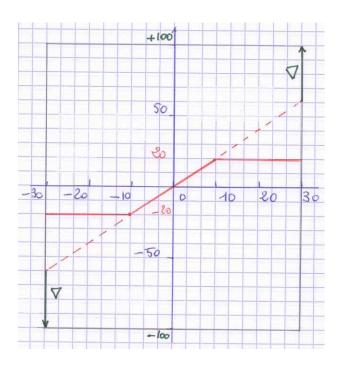
```
if (B)
   { X=0; Y=1; }
else
   { X=1; Y=0; }
R = 1 / (X-Y);
```

cannot result in a division by zero

Case analysis with loop unrolling

– Code Sample:

```
/* trace_partitionning.c */
void main() {
  float t[5] = {-10.0, -10.0, 0.0, 10.0, 10.0};
  float c[4] = {0.0, 2.0, 2.0, 0.0};
  float d[4] = {-20.0, -20.0, 0.0, 20.0};
  float x, r;
  int i = 0;
  __ASTREE_known_fact(((-30.0 <= x) && (x <= 30.0)));
  while ((i < 3) && (x >= t[i+1])) {
    i = i + 1;
  }
  r = (x - t[i]) * c[i] + d[i];
  __ASTREE_log_vars((r));
}
```







The Astrée static analyzer

http://www.astree.ens.fr/

Project Members



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Xavier RIVAL

⁷ Nov. 2001 — Aug. 2007.











⁶ Nov. 2001 — Nov. 2003.

Programs Analyzed by ASTRÉE and their Semantics



Programs analysed by ASTRÉE

- Application Domain: large safety critical embedded real-time synchronous software for non-linear control of very complex control/command systems.
- C programs:
 - with
 - · basic numeric datatypes, structures and arrays
 - · pointers (including on functions),
 - · floating point computations
 - · tests, loops and function calls
 - · limited branching (forward goto, break, continue)



- with (cont'd)
 - union ù NEW [Min06a]
 - pointer arithmetics & casts [Min06a]
- without
 - dynamic memory allocation
 - recursive function calls
 - unstructured/backward branching
 - conflicting side effects
 - C libraries, system calls (parallelism)

Such limitations are quite common for embedded safety-critical software.



The Class of Considered Periodic Synchronous Programs

```
declare volatile input, state and output variables;
initialize state and output variables;
loop forever
   - read volatile input variables,
   - compute output and state variables,
   - write to output variables;
   __ASTREE_wait_for_clock();
end loop
```

Task scheduling is static:

- Requirements: the only interrupts are clock ticks;
- Execution time of loop body less than a clock tick, as verified by the aiT WCET Analyzers [FHL⁺01].

Concrete Operational Semantics

- International norm of C (ISO/IEC 9899:1999)
- restricted by implementation-specific behaviors depending upon the machine and compiler (e.g. representation and size of integers, IEEE 754-1985 norm for floats and doubles)
- restricted by user-defined programming guidelines (such as no modular arithmetic for signed integers, even though this might be the hardware choice)
- restricted by program specific user requirements (e.g. assert, execution stops on first runtime error 8)

⁸ semantics of C unclear after an error, equivalent if no alarm





Different Classes of Run-time Errors

- 1. Errors terminating the execution 9. Astrée warns and continues by taking into account only the executions that did not trigger the error.
- 2. Errors not terminating the execution with predictable outcome ¹⁰. Astrée warns and continues with worst-case assumptions.
- 3. Errors not terminating the execution with unpredictable outcome 11. Astrée warns and continues by taking into account only the executions that did not trigger the error.
- ⇒ ASTRÉE is sound with respect to C standard, unsound with respect to C implementation, unless no false alarm.

¹¹ e.g. memory corruptionss.





⁹ floating-point exceptions e.g. (invalid operations, overflows, etc.) when traps are activated

¹⁰ e.g. overflows over signed integers resulting in some signed integer.

Specification Proved by Astrée





Implicit Specification: Absence of Runtime Errors

- No violation of the norm of C (e.g. array index out of bounds, division by zero)
- No implementation-specific undefined behaviors (e.g. maximum short integer is 32767, NaN)
- No violation of the programming guidelines (e.g. static variables cannot be assumed to be initialized to 0)
- No violation of the programmer assertions (must all be statically verified).



Modular Arithmetic



Modular arithmetics is not very intuitive

In C:

```
% cat -n modulo-c.c
     1 #include <stdio.h>
     2 int main () {
     3 \text{ int } x,y;
     4 \times = -2147483647 / -1;
     5 y = ((-x) -1) / -1;
     6 printf("x = \%i, y = \%i\n",x,y);
     7 }
     8
% gcc modulo-c.c
% ./a.out
x = 2147483647, y = -2147483648
```



Static Analysis with Astrée

```
% cat -n modulo.c
     1 int main () {
     2 int x,y;
     3 \times = -2147483647 / -1;
     4 y = ((-x) -1) / -1;
     5 __ASTREE_log_vars((x,y));
     6 }
% astree -exec-fn main -unroll 0 modulo.c\
 |& egrep -A 1 "(<integers)|(WARN)"
modulo.c:4.4-18::[call#main@1:]: WARN: signed int arithmetic range
  {2147483648} not included in [-2147483648, 2147483647]
  <integers (intv+cong+bitfield+set): y in [-2147483648, 2147483647] /\ Top</pre>
   x in \{2147483647\} / \{2147483647\} >
```

ASTRÉE signals the overflow and goes on with an unkown value.





Float Overflow





Float Arithmetics does Overflow

In C:

```
% cat -n overflow.c
                                    % astree -exec-fn main
                                     overflow.c |& grep "WARN"
 1 void main () {
                                     overflow.c:3.4-23::[call#main1:]:
   double x,y;
                                     WARN: double arithmetic range
 3 \times = 1.0e + 256 \times 1.0e + 256;
                                     [1.79769e+308, inf] not
   y = 1.0e+256 * -1.0e+256;
                                     included in [-1.79769e+308,
   __ASTREE_log_vars((x,y));
                                     1.79769e+3087
                                     overflow.c:4.4-24::[call#main1:]:
                                     WARN: double arithmetic range
% gcc overflow.c
                                     [-inf, -1.79769e+308] not
% ./a.out
                                     included in [-1.79769e+308,
x = \inf, y = -\inf
                                     1.79769e+3081
```

The Ariane 5.01 maiden flight

- June 4^{th} , 1996 was the maiden flight of Ariane 5



The Ariane 5.01 maiden flight failure

- June 4th, 1996 was the maiden flight of Ariane 5
- The launcher was detroyed after 40 seconds of flight because of a software overflow 12



¹² A 16 bit piece of code of Ariane 4 had been reused within the new 32 bit code for Ariane 5. This caused an uncaught overflow, making the launcher uncontrolable.





Rounding





Example of rounding error

```
/* float-error.c */
int main () {
  float x, y, z, r;
 x = 1.00000019e+38;
 y = x + 1.0e21;
 z = x - 1.0e21;
 r = y - z;
 printf("%f\n", r);
% gcc float-error.c
% ./a.out
0.00000
```

```
/* double-error.c */
int main () {
double x; float y, z, r;
/* x = 1dexp(1.,50) + 1dexp(1.,26); */
x = 1125899973951488.0;
y = x + 1;
z = x - 1:
r = y - z;
printf("%f\n", r);
% gcc double-error.c
% ./a.out
134217728.000000
```

$$(x+a)-(x-a)\neq 2a$$





Example of rounding error

```
/* float-error.c */
int main () {
  float x, y, z, r;
 x = 1.00000019e+38;
 y = x + 1.0e21;
 z = x - 1.0e21;
 r = y - z;
 printf("%f\n", r);
% gcc float-error.c
% ./a.out
0.00000
```

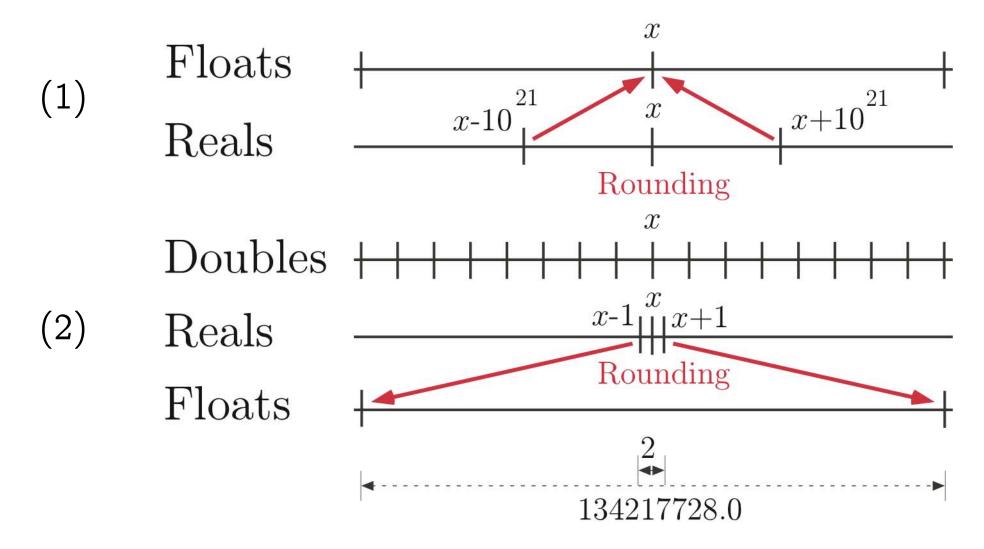
```
/* double-error.c */
int main () {
double x; float y, z, r;
/* x = 1dexp(1.,50) + 1dexp(1.,26); */
x = 1125899973951487.0;
y = x + 1;
z = x - 1:
r = y - z;
printf("%f\n", r);
% gcc double-error.c
% ./a.out
0.00000
```

$$(\mathbf{x}+\mathbf{a})-(\mathbf{x}-\mathbf{a})\neq 2\mathbf{a}$$





Explanation of the huge rounding error



Static analysis with Astrée 13

```
% cat -n double-error.c
 2 int main () {
 3 double x; float y, z, r;;
 4 /* x = ldexp(1.,50) + ldexp(1.,26); */
 5 \times 1125899973951488.0;
 6 y = x + 1;
7 z = x - 1;
8 r = y - z;
 9 __ASTREE_log_vars((r));
10 }
% gcc double-error.c
% ./a.out
134217728.000000
% astree -exec-fn main -print-float-digits 10 double-error.c |& grep "r in
direct = <float-interval: r in [-134217728, 134217728] >
```

¹³ Astrée makes a worst-case assumption on the rounding $(+\infty, -\infty, 0, \text{ nearest})$ hence the possibility to get -134217728.





Example of accumulation of small rounding errors

```
% cat -n rounding-c.c
 1 #include <stdio.h>
 2 int main () {
 3 int i; double x; x = 0.0;
 4 for (i=1; i<=100000000; i++) {
 5 \quad x = x + 1.0/10.0;
 7 printf("x = %f \ x);
% gcc rounding-c.c
% ./a.out
x = 99999998.745418
```

since $(0.1)_{10} = (0.0001100110011001100...)_2$





Static analysis with Astrée

```
% cat -n rounding.c
     1 int main () {
        double x; x = 0.0;
     3 while (1) {
     4 	 x = x + 1.0/10.0;
     5 __ASTREE_log_vars((x));
     6 __ASTREE_wait_for_clock(());
% cat rounding.config
 __ASTREE_max_clock((100000000));
% astree -exec-fn main -config-sem rounding.config -unroll 0 rounding.c\
 |\& egrep "(x in)|(\|x\|)|(WARN)" | tail -2
direct = <float-interval: x in [0.1, 200000040.938] >
  |x| \le 1.*((0. + 0.1/(1.-1))*(1.)^{clock} - 0.1/(1.-1)) + 0.1
      <= 200000040.938
```

The Patriot missile failure

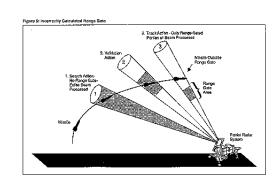
- "On February 25th, 1991, a Patriot missile ... failed to track and intercept an incoming Scud (*)."
- The software failure was due to accumulated rounding error (†)



^(*) This Scud subsequently hit an Army barracks, killing 28 Americans.

- (†) "Time is kept continuously by the system's internal clock in tenths of seconds"
 - "The system had been in operation for over 100 consecutive hours"
 - "Because the system had been on so long, the resulting inaccuracy in the time calculation caused the range gate to shift so much that the system could not track the incoming Scud"

SoLA 2007, LISI, Poitiers, 12/12/2007







Scaling







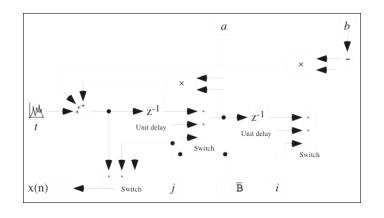
Static Analysis of Scaling with Astrée

```
% cat -n scale.c
                                  % gcc scale.c
                                % ./a.out
 1 int main () {
 2 float x; x = 0.70000001; x = 0.69999988079071
 3 while (1) {
 4 \quad x = x / 3.0;
 5 \quad x = x * 3.0;
 6 __ASTREE_log_vars((x));
   __ASTREE_wait_for_clock(());
 8 }
 9 }
% cat scale.config
 __ASTREE_max_clock((100000000));
% astree -exec-fn main -config-sem scale.config -unroll 0 scale.c\
 |& grep "x in" | tail -1
direct = \langle float-interval: x in [0.69999986887, 0.700000047684] >
```



Filtering

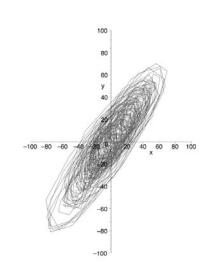
2^d Order Digital Filter:



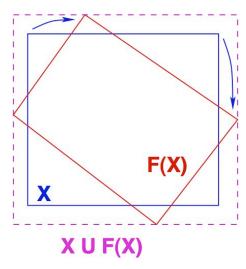
Ellipsoid Abstract Domain for Filters

- Computes
$$X_n = \left\{ egin{array}{l} lpha X_{n-1} + eta X_{n-2} + Y_n \ I_n \end{array}
ight.$$

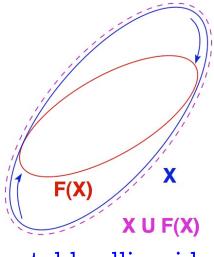
- The concrete computation is bounded, which must be proved in the abstract.
- There is no stable interval or octagon.
- The simplest stable surface is an ellipsoid.



execution trace



unstable interval



stable ellipsoid



Filter Example [Fer04]

```
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
BOOLEAN INIT; float P, X;
void filter () {
  static float E[2], S[2];
  if (INIT) { S[O] = X; P = X; E[O] = X; }
  else { P = (((((0.5 * X) - (E[0] * 0.7)) + (E[1] * 0.4))
             + (S[0] * 1.5)) - (S[1] * 0.7)); }
  E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;
  /* S[0], S[1] in [-1327.02698354, 1327.02698354] */
}
void main () { X = 0.2 * X + 5; INIT = TRUE;
  while (1) {
    X = 0.9 * X + 35; /* simulated filter input */
    filter (); INIT = FALSE; }
}
```

Time Dependence



Arithmetic-Geometric Progressions (Example 1)

```
% cat count.c
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
volatile BOOLEAN I; int R; BOOLEAN T;
void main() {
 R = 0;
  while (TRUE) {
    __ASTREE_log_vars((R));
                                  ← potential overflow!
    if (I) \{ R = R + 1; \}
    else { R = 0; }
    T = (R >= 100);
    __ASTREE_wait_for_clock(());
  }}
% cat count.config
__ASTREE_volatile_input((I [0,1]));
__ASTREE_max_clock((3600000));
% astree -exec-fn main -config-sem count.config count.c|grep '|R|'
|R| \le 0. + clock *1. \le 3600001.
```



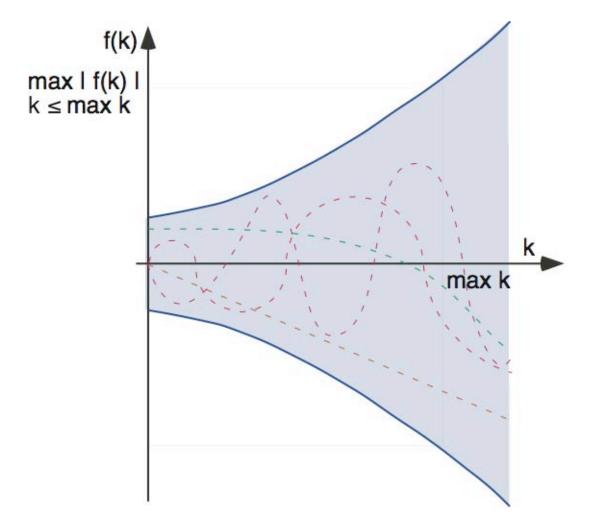




Arithmetic-Geometric Progressions: Example 2

```
% cat retro.c
                                         void main()
typedef enum {FALSE=0, TRUE=1} BOOL;
                                         { FIRST = TRUE;
BOOL FIRST;
                                           while (TRUE) {
volatile BOOL SWITCH;
                                             dev();
volatile float E;
                                             FIRST = FALSE;
float P, X, A, B;
                                             ASTREE wait for clock(());
                                           }}
void dev( )
                                         % cat retro.config
\{ X=E;
                                         __ASTREE_volatile_input((E [-15.0, 15.0]));
  if (FIRST) { P = X; }
                                         __ASTREE_volatile_input((SWITCH [0,1]));
  else
                                         __ASTREE_max_clock((3600000));
    \{ P = (P - ((((2.0 * P) - A) - B)) \}
                                         |P| \le (15. + 5.87747175411e-39)
            * 4.491048e-03)); };
                                         / 1.19209290217e-07) * (1
  B = A;
                                         + 1.19209290217e-07)^clock
  if (SWITCH) \{A = P;\}
                                        - 5.87747175411e-39 /
  else \{A = X;\}
                                         1.19209290217e-07 <= 23.0393526881
```

Overapproximation with an Arithmetic-Geometric Progression









Arithmetic-geometric progressions ¹⁴ [Fer05]

- Abstract domain: $(\mathbb{R}^+)^5$
- Concretization:

$$\gamma \in (\mathbb{R}^+)^5 \longmapsto \wp(\mathbb{N} \mapsto \mathbb{R})$$

$$\gamma(M,a,b,a',b') =$$

$$\{f \mid orall k \in \mathbb{N} : |f(k)| \leq \left(oldsymbol{\lambda} \, x ullet ax + b \circ \left(oldsymbol{\lambda} \, x ullet a'x + b'
ight)^k
ight)(M)\}$$

i.e. any function bounded by the arithmetic-geometric progression.

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¹⁴ In Fleet In The arithmetic-geometric progression abstract domain. In VMCAI'05, Paris, LNCS 3385, pp. 42-58, Springer, 2005.









The industrial use of Astrée

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D. Delmas and J. Souyris. ASTRÉE: from Research to Industry. Proc. 14th Int. Symp. SAS '07, G. Filé and H. Riis-Nielson (eds), 22-24 Aug. 2007, Kongens Lyngby, DK, LNCS 4634, pp. 437-451, Springer.





Example application

 Primary flight control software of the Airbus A340 family/A380 fly-by-wire system





- C program, automatically generated from a proprietary high-level specification (à la Simulink/SCADE)
- A340 family: 132,000 lines, 75,000 LOCs after preprocessing, 10,000 global variables, over 21,000 after expansion of small arrays, now \times 2
- $A380: \times 3/7$



Digital Fly-by-Wire Avionics 15



The electrical flight control system is placed between the pilot's controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement they control and monitor.









Benchmarks (Airbus A340 Primary Flight Control Software)

- V1¹⁶, 132,000 lines, 75,000 LOCs after preprocessing
- Comparative results (commercial software):
 4,200 (false?) alarms, 3.5 days;
- Our results:

 $\underline{\mathbf{0}}$ alarms,

40mn on 2.8 GHz PC, 300 Megabytes

→ A world première in Nov. 2003!

¹⁶ "Flight Control and Guidance Unit" (FCGU) running on the "Flight Control Primary Computers" (FCPC). The three primary computers (FCPC) and two secondary computers (FCSC) which form the A340 and A330 electrical flight control system are placed between the pilot's controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement they control and monitor.





The main loop invariant for the A340 V1

A textual file over 4.5 Mb with

- -6,900 boolean interval assertions ($x \in [0;1]$)
- -9,600 interval assertions ($x \in [a;b]$)
- -25,400 clock assertions $(x+\operatorname{clk} \in [a;b] \land x-\operatorname{clk} \in [a;b])$
- -19,100 additive octagonal assertions $(a \le x + y \le b)$
- -19,200 subtractive octagonal assertions $(a \le x y \le b)$
- 100 decision trees
- 60 ellipse invariants, etc . . .

involving over 16,000 floating point constants (only 550 appearing in the program text) \times 75,000 LOCs.



(Airbus A380 Primary Flight Control Software)

- U alarms (Nov. 2004), after some additional parametrization and simple abstract domains developments
- Now at 1,000,000 lines!

34h,

8 Gigabyte

→ A world grand première!



Possible origins of imprecision and how to fix it

In case of false alarm, the imprecision can come from:

- Abstract transformers (not best possible) —> improve algorithm;
- Automatized parametrization (e.g. variable packing)
 improve pattern-matched program schemata;
- Iteration strategy for fixpoints → fix widening ¹⁷;
- Inexpressivity i.e. indispensable local inductive invariant are inexpressible in the abstract → add a new abstract domain to the reduced product (e.g. filters).

¹⁷ This can be very hard since at the limit only a precise infinite iteration might be able to compute the proper abstract invariant. In that case, it might be better to design a more refined abstract domain.





5. Conclusion



Characteristics of the Astrée Analyzer

Sound: - Astrée is a bug eradicator: finds all bugs in a well-defined class (runtime errors)

- Astrée is not a bug hunter: finding some bugs in a well-defined class (e.g. by bug pattern detection like FindBugs[™], PREfast or PMD)
- Astrée is exhaustive: covers the whole state space (\neq MAGIC, CBMC)
- Astrée is comprehensive: never omits potential errors (\neq UNO, CMC from coverity.com) or sort most probable ones to avoid overwhelming messages (\neq Splint)



Static: compile time analysis (\neq run time analysis Rational Purify, Parasoft Insure++)

Program Analyzer: analyzes programs not micromodels of programs (\neq PROMELA in SPIN or Alloy in the Alloy Analyzer)

Automatic: no end-user intervention needed (\neq ESC Java, ESC Java 2), or PREfast (annotate functions with intended use)



Multiabstraction: uses many numerical/symbolic abstract domains (\neq symbolic constraints in Bane or the canonical abstraction of TVLA)

Infinitary: all abstractions use infinite abstract domains with widening/narrowing (\neq model checking based analyzers such as Bandera, Bogor, Java PathFinder, Spin, VeriSoft)

Efficient: always terminate (\neq counterexample-driven automatic abstraction refinement BLAST, SLAM)



Extensible/Specializable: can easily incorporate new abstractions (and reduction with already existing abstract domains) (\neq general-purpose analyzers PolySpace Verifier)

Domain-Aware: knows about control/command (e.g. digital filters) (as opposed to specialization to a mere programming style in C Global Surveyor)

Parametric: the precision/cost can be tailored to user needs by options and directives in the code



Automatic Parametrization: the generation of parametric directives in the code can be programmed (to be specialized for a specific application domain)

Modular: an analyzer instance is built by selection of O-CAML modules from a collection each implementing an abstract domain



The Future of the Astrée Analyzer

- ASTRÉE has shown usable and useful in one industrial context (*electric flight control*):
 - as a R & D tool for A340 V2 and A380,
 - as a production tool for the A350;
- More applications are forthcoming (ES_PASS project);
- Industrialization is simultaneously under consideration.



THE END, THANK YOU



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