

Verification by Abstract Interpretation

Patrick COUSOT
École Normale Supérieure
45 rue d'Ulm
75230 Paris cedex 05, France
Patrick.Cousot@ens.fr
www.di.ens.fr/~cousot

Università degli Studi di Verona
Verona, Italy
September 2nd, 2004, 17:00–18:00

Talk Outline

- A short introduction to abstract interpretation
(15 mn) 3
- Example: predicate abstraction (10 mn) 18
- Generic abstraction (15 mn) 27
- Application to the verification of embedded, real-time, synchronous, safety super-critical software (10 mn) 36
- Conclusion (5 mn) 46



A Short Introduction to Abstract Interpretation (based on [POPL '79, Sec. 5])

Reference

[POPL '79] P. Cousot & R. Cousot. Systematic design of program analysis frameworks. In *6th POPL*, pages 269–282, San Antonio, TX, 1979. ACM Press.



Complete Lattice of Properties

- We represent **properties** P of objects $s \in \Sigma$ as **sets of objects** $P \in \wp(\Sigma)$ (which have the property in question);

Example: the property “*to be an even natural number*” is $\{0, 2, 4, 6, \dots\}$

- The **set of properties** of objects Σ is a complete boolean lattice:

$$\langle \wp(\Sigma), \subseteq, \emptyset, \Sigma, \cup, \cap, \neg \rangle .$$



Abstraction

A reasoning/computation such that:

- only some properties can be used;
- the properties that can be used are called “*abstract*”;
- so, the (other *concrete*) properties must be approximated by the abstract ones;



Abstract Properties

- **Abstract Properties:** a set $\overline{\mathcal{A}} \subseteq \wp(\Sigma)$ of properties of interest (the only one which can be used to approximate others).

Direction of Approximation

- **Approximation from above:** approximate P by \overline{P} such that $P \subseteq \overline{P}$;
- **Approximation from below:** approximate P by \underline{P} such that $\underline{P} \subseteq P$ (**dual**).



Best Abstraction

- We require that all concrete property $P \in \wp(\Sigma)$ have a best abstraction $\overline{P} \in \overline{\mathcal{A}}$:

$$\begin{gathered} P \subseteq \overline{P} \\ \forall \overline{P'} \in \overline{\mathcal{A}} : (P \subseteq \overline{P'}) \Rightarrow (\overline{P} \subseteq \overline{P'}) \end{gathered}$$

- So, by definition of the greatest lower bound/meet \cap :

$$\overline{P} = \bigcap \{ \overline{P'} \in \overline{\mathcal{A}} \mid P \subseteq \overline{P'} \} \in \overline{\mathcal{A}}$$

(Otherwise see [JLC '92].)



Reference

[JLC'92] P. Cousot & R. Cousot. Abstract interpretation frameworks. *J. Logic and Comp.*, 2(4):511–547, 1992.



Moore Family

- This hypothesis that any concrete property $P \in \wp(\Sigma)$ has a best abstraction $\overline{P} \in \overline{\mathcal{A}}$ implies that:

$\overline{\mathcal{A}}$ is a Moore family

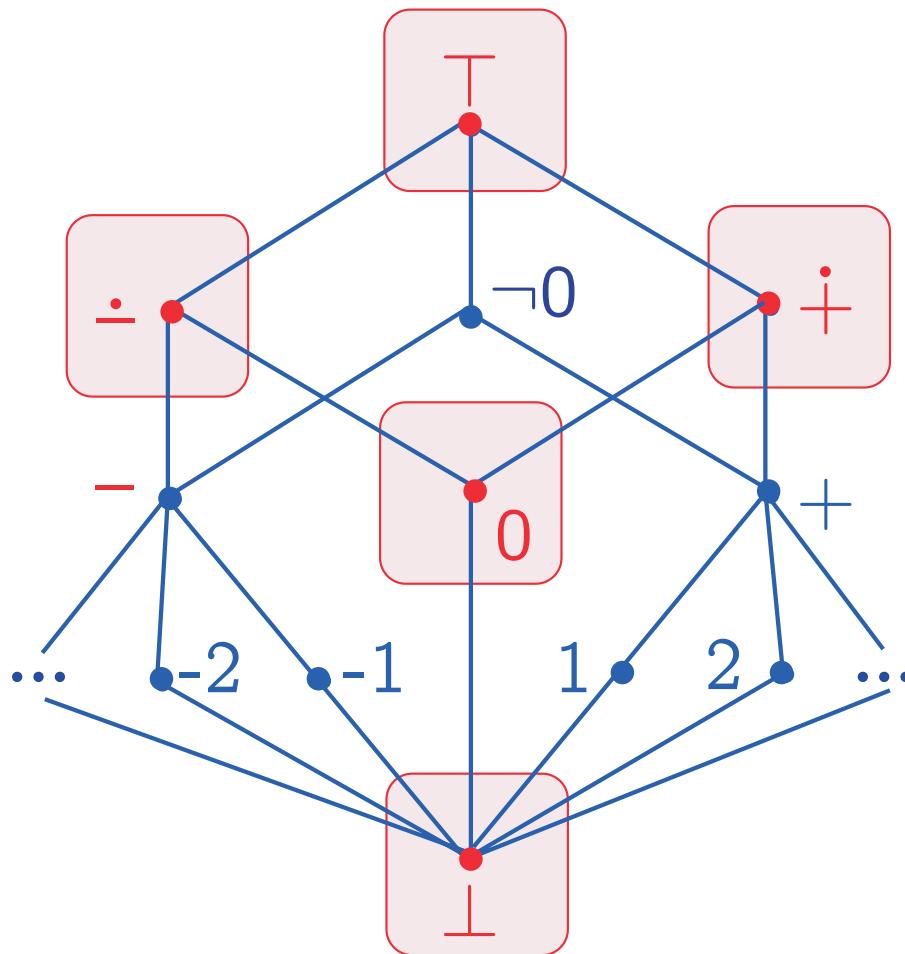
i.e. it is closed under intersection \cap :

$$\forall S \subseteq \overline{\mathcal{A}} : \cap S \in \overline{\mathcal{A}}$$

- In particular $\cap \emptyset = \Sigma \in \overline{\mathcal{A}}$ is “I don’t know”.



Example of Moore Family-Based Abstraction



Closure Operator Induced by an Abstraction

The map $\rho_{\bar{\mathcal{A}}}$ mapping a concrete property $P \in \wp(\Sigma)$ to its best abstraction $\rho_{\bar{\mathcal{A}}}(P)$ in $\bar{\mathcal{A}}$:

$$\rho_{\bar{\mathcal{A}}}(P) = \bigcap \{\bar{P} \in \bar{\mathcal{A}} \mid P \subseteq \bar{P}\}$$

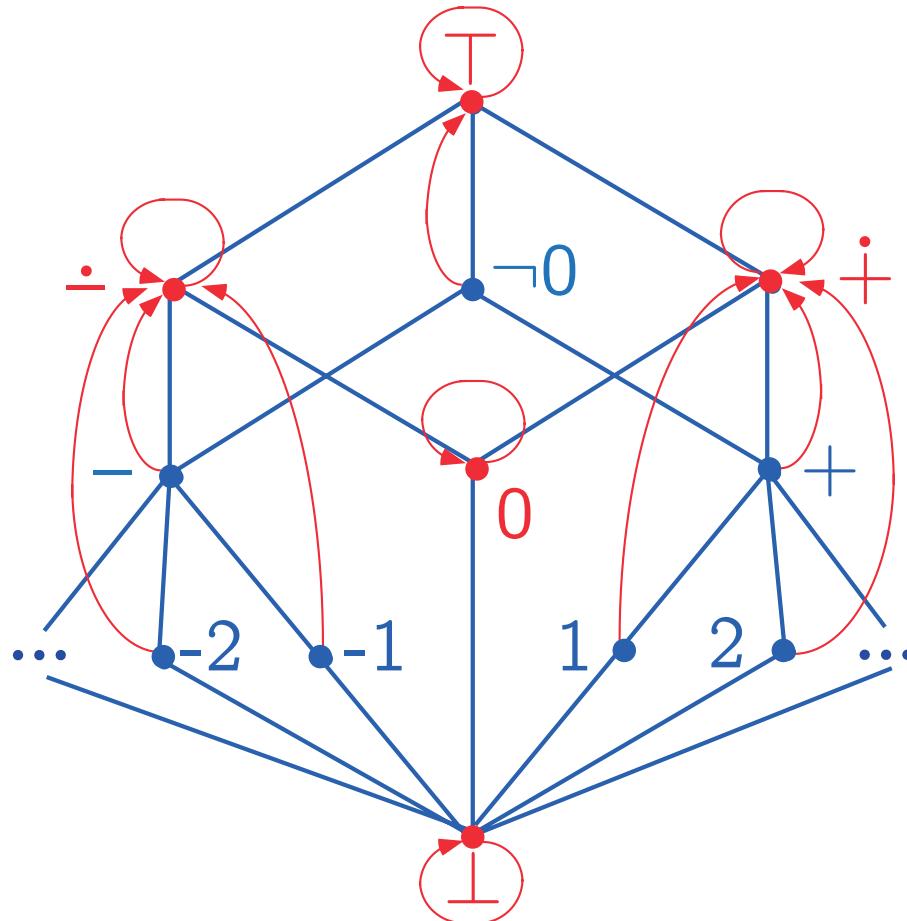
is a **closure operator**:

- extensive,
- idempotent,
- isotone/monotonic;

such that $P \in \bar{\mathcal{A}} \iff P = \rho_{\bar{\mathcal{A}}}(P)$
hence $\bar{\mathcal{A}} = \rho_{\bar{\mathcal{A}}}(\wp(\Sigma))$.



Example of Closure Operator-Based Abstraction



Galois Connection Between Concrete and Abstract Properties

- For closure operators ρ , we have:

$$\rho(P) \subseteq \rho(P') \Leftrightarrow P \subseteq \rho(P')$$

written:

$$\langle \wp(\Sigma), \subseteq \rangle \xrightleftharpoons[\rho]{1} \langle \rho(\wp(\Sigma)), \subseteq \rangle$$

where 1 is the identity and:

$$\langle \wp(\Sigma), \subseteq \rangle \xrightleftharpoons[\alpha]{\gamma} \langle \overline{\mathcal{D}}, \sqsubseteq \rangle$$

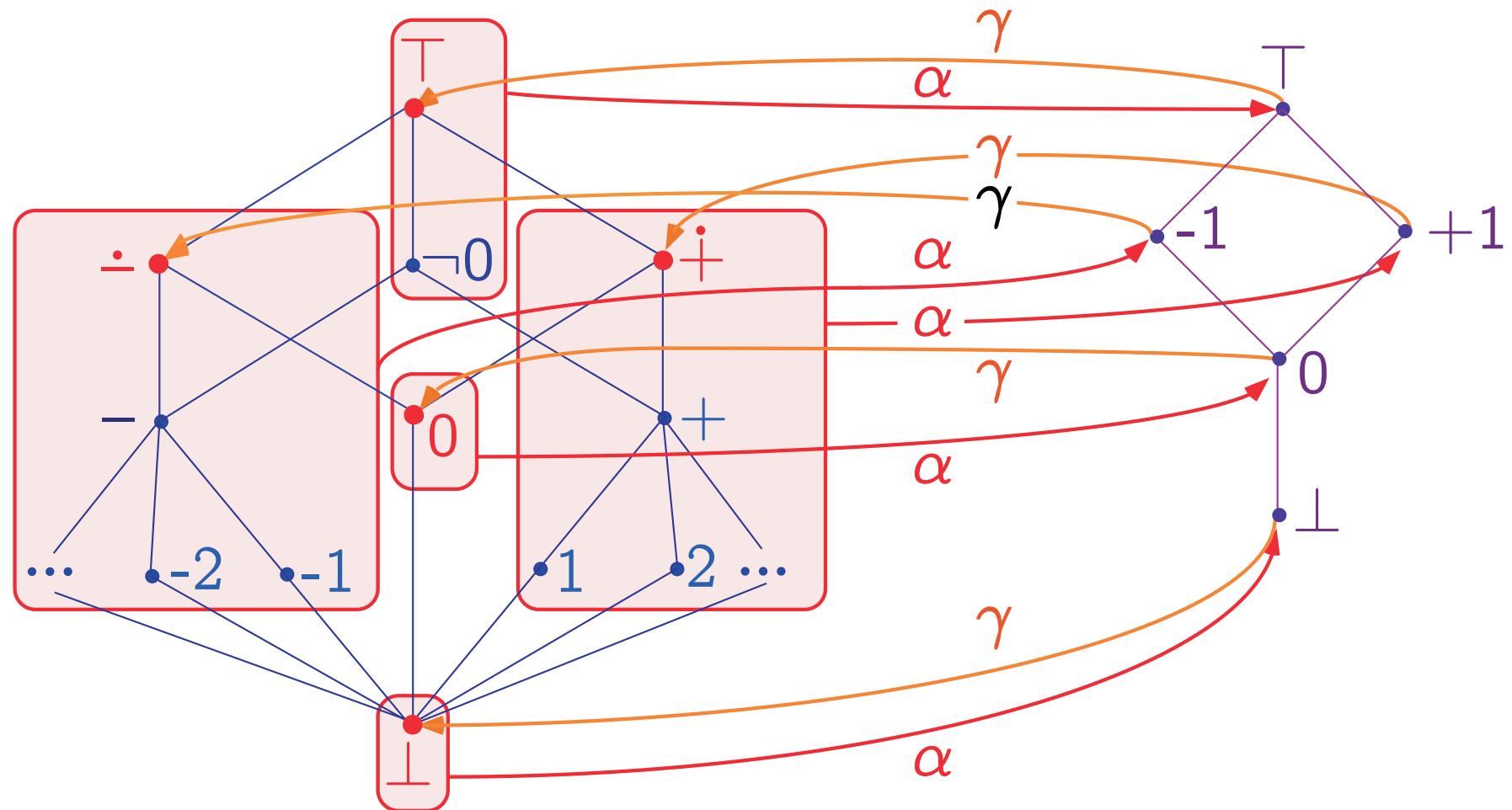
means that $\langle \alpha, \gamma \rangle$ is a **Galois connection**:

$$\forall P \in \wp(\Sigma), \overline{P} \in \overline{\mathcal{D}} : \alpha(P) \sqsubseteq \overline{P} \Leftrightarrow P \subseteq \gamma(\overline{P});$$

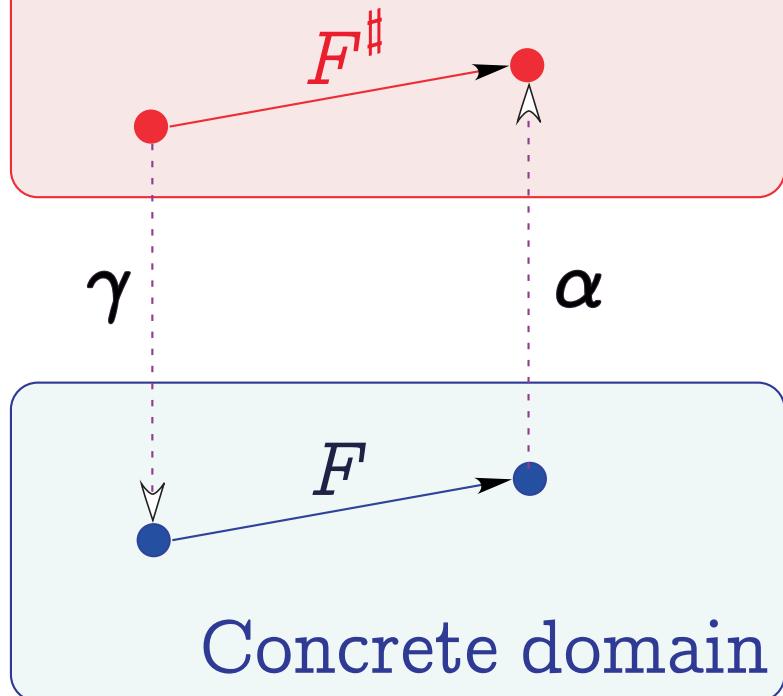
- A Galois connection defines a closure operator $\rho = \alpha \circ \gamma$, hence a best abstraction.



Example of Galois Connection-Based Abstraction



Abstract domain



Function Abstraction

$$F^\sharp = \alpha \circ F \circ \gamma$$

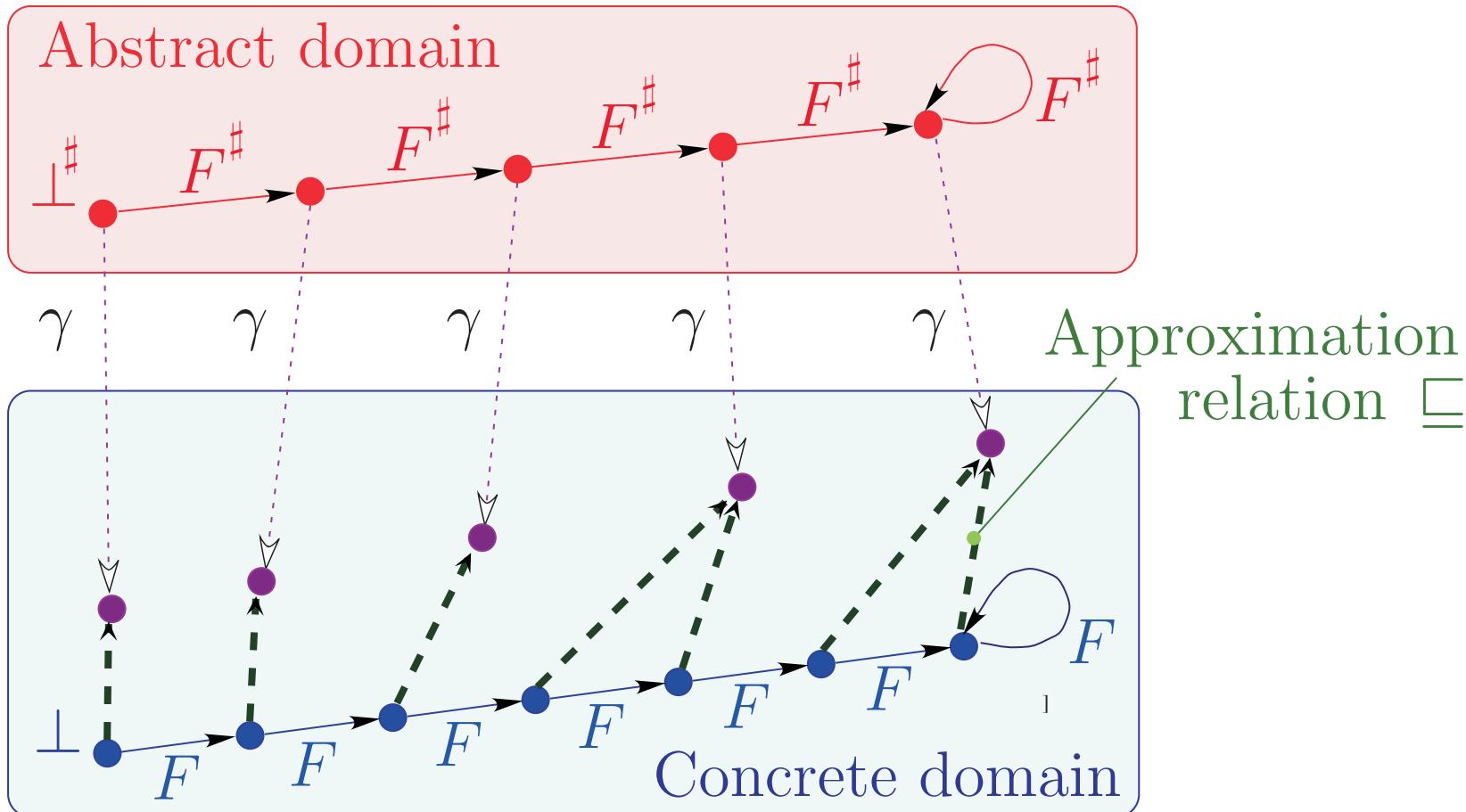
.e. $F^\sharp = \rho \circ F$

$$\langle P, \subseteq \rangle \xrightleftharpoons[\alpha]{\gamma} \langle Q, \sqsubseteq \rangle \Rightarrow$$

$$\langle P \xrightarrow{\text{mon}} P, \dot{\subseteq} \rangle \xrightleftharpoons[\lambda F . \alpha \circ F \circ \gamma]{\lambda F^\sharp . \gamma \circ F^\sharp \circ \alpha} \langle Q \xrightarrow{\text{mon}} Q, \dot{\sqsubseteq} \rangle$$



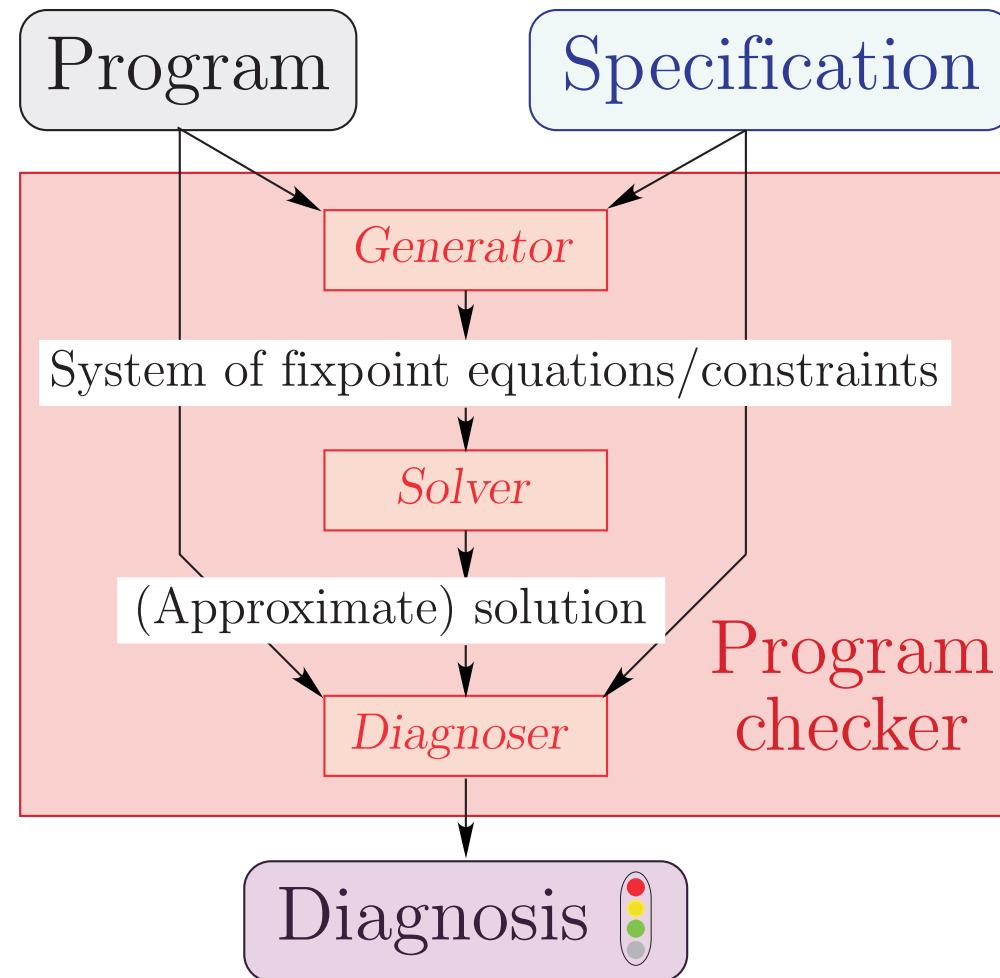
Approximate Fixpoint Abstraction



$$F \circ \gamma \sqsubseteq \gamma \circ F^\sharp \Rightarrow \text{lfp } F \sqsubseteq \gamma(\text{lfp } F^\sharp)$$



Program Checking by Static Analysis



Application to Predicate Abstraction

Reference

- [1] S. Graf and H. Saïdi. Construction of abstract state graphs with PVS. In *Proc. 9th Int. Conf. CAV '97*, LNCS 1254, pp. 72–83. Springer, 1997.



The Structure of Program States

- States: $\Sigma = \mathcal{L} \times \mathcal{M}$
- Program points/labels: \mathcal{L} is finite
- Variables: \mathbb{X} is finite (for a given program)
- Set of values: \mathcal{V}
- Memory states: $\mathcal{M} = \mathbb{X} \mapsto \mathcal{V}$

Program Properties¹

$$P \in \wp(\mathcal{L} \times \mathcal{M})$$

¹ e.g. for reachability.



Local Versus Global Assertions

- Isomorphism between global and local assertions:

$$\langle \wp(\mathcal{L} \times \mathcal{M}), \subseteq \rangle \xrightleftharpoons[\alpha_\downarrow]{\gamma_\downarrow} \langle \mathcal{L} \mapsto \wp(\mathcal{M}), \dot{\subseteq} \rangle$$

where:

$$\begin{aligned}\alpha_\downarrow(P) &= \lambda l. \{m \mid \langle l, m \rangle \in P\} \\ \gamma_\downarrow(Q) &= \{\langle l, m \rangle \mid l \in \mathcal{L} \wedge m \in Q_l\}\end{aligned}$$

and $\dot{\subseteq}$ is the pointwise ordering:

$$Q \dot{\subseteq} Q' \text{ if and only if } \forall l \in \mathcal{L} : Q_l \subseteq Q'_l.$$



Syntactic Predicates

- Choose a set \mathbb{P} of syntactic predicates p such that:

$$\forall S \subseteq \mathbb{P} : (\bigwedge S) \in \mathbb{P}$$

- an interpretation $\mathcal{I} \in \mathbb{P} \mapsto \wp(\mathcal{M})$ such that:

$$\forall S \subseteq \mathbb{P} : \mathcal{I}(\bigwedge S) = \bigcap_{p \in S} \mathcal{I}[p]$$

- It follows that $\{\mathcal{I}[p] \mid p \in \mathbb{P}\}$ is a Moore family.



Predicate Abstraction

A memory state property $Q \in \wp(\mathcal{M})$ is approximated by the subset of predicates p of \mathbb{P} which holds when Q holds (formally $Q \subseteq \mathcal{I}[p]$). This defines a Galois connection:

$$\langle \wp(\mathcal{M}), \subseteq \rangle \xleftrightarrow{\alpha_{\mathbb{P}}} \langle \wp(\mathbb{P}), \supseteq \rangle$$

where:

$$\alpha_{\mathbb{P}}(Q) \stackrel{\text{def}}{=} \{p \in \mathbb{P} \mid Q \subseteq \mathcal{I}[p]\}$$

$$\gamma_{\mathbb{P}}(P) \stackrel{\text{def}}{=} \bigcap \{\mathcal{I}[p] \mid p \in P\}$$

(*In practice one uses an isomorphic Boolean encoding*)



Pointwise Extension to All program Points

By pointwise extension, we have for all program points:

$$\langle \mathcal{L} \mapsto \wp(\mathcal{M}), \dot{\subseteq} \rangle \xleftrightarrow[\dot{\alpha}_{\mathbb{P}}]{\dot{\gamma}_{\mathbb{P}}} \langle \mathcal{L} \mapsto \wp(\mathbb{P}), \dot{\supseteq} \rangle$$

where:

$$\dot{\alpha}_{\mathbb{P}}(Q) = \lambda \ell \cdot \alpha_{\mathbb{P}}(Q_{\ell})$$

$$\dot{\gamma}_{\mathbb{P}}(P) = \lambda \ell \cdot \gamma_{\mathbb{P}}(P_{\ell})$$

$$P \dot{\supseteq} P' = \forall \ell \in \mathcal{L} : P_{\ell} \supseteq P'_{\ell}$$



Composition: Pointwise Predicate Abstraction

By composition, we get:

$$\langle \wp(\mathcal{L} \times \mathcal{M}), \subseteq \rangle \xrightleftharpoons[\alpha]{\gamma} \langle \mathcal{L} \mapsto \wp(\mathbb{P}), \dot{\supseteq} \rangle$$

where:

$$\alpha(P) = \dot{\alpha}_{\mathbb{P}} \circ \alpha_{\downarrow}(P)$$

$$\gamma(Q) = \gamma_{\downarrow} \circ \dot{\gamma}_{\mathbb{P}}(Q)$$



Abstract Predicate Transformer (Sketchy)

$$\begin{aligned} & \alpha \circ \text{post}[\![X := E]\!] \circ \gamma\left(\bigwedge_{i=1}^n q_i\right) && \text{where } \{q_1, \dots, q_n\} \subseteq \{\mathbf{p}_1, \dots, \mathbf{p}_k\} \\ & = \alpha \circ \text{post}[\![X := E]\!]\left(\bigcap_{i=1}^n \mathcal{I}[\![q_i]\!]\right) && \text{def. } \gamma \\ & = \alpha(\{\rho[X/\![E]\!\rho] \mid \rho \in \bigcap_{i=1}^n \mathcal{I}[\![q_i]\!]\}) && \text{def. post}[\![X := E]\!] \\ & = \alpha(\bigcap_{i=1}^n \mathcal{I}[\![q_i[X/E]]\!]) && \text{def. substitution} \\ & = \bigwedge\{\mathbf{p}_j \mid \mathcal{I}[\![q_i[X/E] \Rightarrow \mathbf{p}_j]\!]\} && \text{def. } \alpha \\ & \Rightarrow \bigwedge\{\mathbf{p}_j \mid \text{theorem_prover}[\![q_i[X/E] \Rightarrow \mathbf{p}_j]\!]\} \end{aligned}$$



since `theorem_prover` $\llbracket q_i[X/E] \Rightarrow p_j \rrbracket$ implies $\mathcal{I}\llbracket q_i[X/E] \Rightarrow p_j \rrbracket$



Generic Abstraction

Reference

[ZM '03] P. Cousot. Verification by Abstract Interpretation. *Proc. Int. Symp. on Verification – Theory & Practice – Honoring Zohar Manna's 64th Birthday*, N. Dershowitz (Ed.), Taormina, Italy, June 29 – July 4, 2003. Lecture Notes in Computer Science, vol. 2772, pp. 243–268. © Springer-Verlag, Berlin, Germany, 2003.



Generic Abstraction in Static Analysis

For **program verification**, one must discover/compute **inductive assertions**.

- **Ground assertions** (e.g. Floyd's invariants on variables attached to program points)
- **Atomic assertions** (e.g. predicate abstraction so the combination with \vee , \wedge , \neg and the localization at program points are automated)
- **Generic assertions** (e.g. parameterized in terms of programs (such as variables))

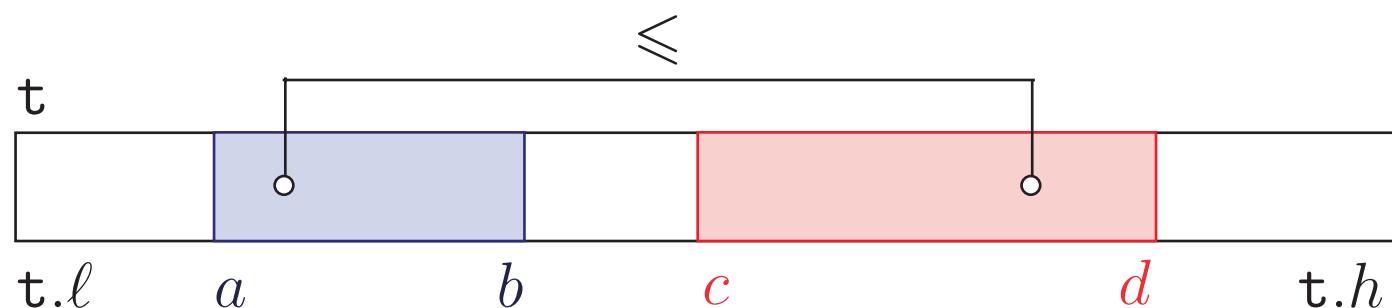
Static analysis:

- **Generic assertions:** Abstract domains
- **Combinations:** Reduced product (\wedge), Disjunctive completion (\vee)



Example of generic abstraction: comparison

- Let $\mathcal{D}_{\text{rel}}(X)$ be a generic relational integer abstract domain parameterized by a set X of variables (e.g. octagons or polyhedra);
- We define the **generic comparison abstract domain**:
$$\mathcal{D}_{\text{lt}}(X) = \{\langle \text{lt}(t, a, b, c, d), r \rangle \mid t \in X \wedge a, b, c, d \notin X \wedge r \in \mathcal{D}_{\text{rel}}(X \cup \{t.\ell, t.h, a, b, c, d\})\}.$$
- Concretization:



Example: Bubble Sort²

```
1 :     var t : array [a, b] of int;
1 :     {a ≤ b}
1 :     I := a;
2 :     {I = a ≤ b}
2 :     wh le (I < b) do
3 :         {lt(t, a, I, I, I) ∧ I < b}
3 :         f (t[I] > t[I + 1]) then
4 :             {lt(t, a, I, I, I) ∧ I < b ∧ lt(t, I, I + 1, I, I)}
4 :             t[I] :=: t[I + 1]
5 :             {lt(t, a, I + 1, I + 1, I + 1) ∧ I + 1 ≤ b}
5 :             fi;
6 :             {lt(t, a, I + 1, I + 1, I + 1) ∧ I + 1 ≤ b}
6 :             I := I + 1
7 :             {lt(t, a, I, I, I) ∧ I ≤ b}
7 :         od
8 :         {lt(t, a, I, I, I) ∧ I = b ∧ s(t, a, b)}
```

² Implementation by Pavol Černy.

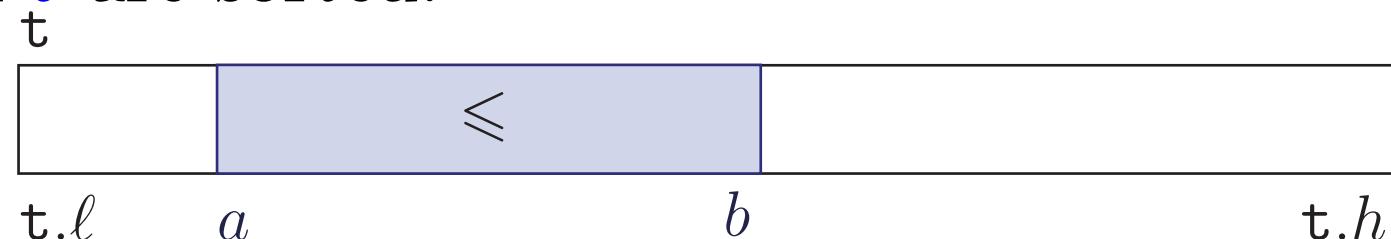


Example of generic abstraction: sorted

- Then we define the generic sorting abstract domain:

$$\mathcal{D}_s(X) = \{\langle s(t, a, b), r \rangle \mid t \in X \wedge a, b \notin X \wedge r \in \mathcal{D}_{\text{rel}}(X \cup \{t.l, t.h, a, b\})\}.$$

- The meaning $\gamma(\langle s(t, a, b), r \rangle)$ of an abstract predicate $\langle s(t, a, b), r \rangle$ is that the elements of t between indices a and b are sorted:



$$\begin{aligned}\gamma(\langle s(t, a, b), r \rangle) = & \exists a, b : t.l \leq a \leq b \leq t.h \wedge \\ & \forall i, j \in [a, b] : (i \leq j) \Rightarrow (t[i] \leq t[j]) \wedge r.\end{aligned}$$



Generic abstract domains

- The comparison and sorted abstract domains are equipped with an implication (partial ordering), a disjunction (lub), a widening and abstract strongest postcondition transformers (assignment, test)



Reduced product

- A reduction operator is defined between the two abstract domains such as, e.g.:

$$\begin{aligned} & \text{lt}(t, a, b - 1, b - 1, b - 1) \wedge \text{lt}(t, a, b, b, b) \\ & \Rightarrow s(t, b - 1, b) \wedge \text{lt}(t, a, b - 1, b - 1, b) \end{aligned}$$

$$\begin{aligned} & s(t, b + 1, c) \wedge \text{lt}(t, a, b + 1, b + 1, c) \wedge \text{lt}(t, a, b, b, b) \\ & \Rightarrow s(t, b, c) \wedge \text{lt}(t, a, b, b, c) \end{aligned}$$

$$\text{lt}(t, a, a + 1, a + 1, b) \wedge s(t, a + 1, b) \Rightarrow s(t, a, b)$$



Abstract invariants

- The invariants are computed by fixpoint iteration with convergence acceleration by widening



Example: Bubble Sort³

```
1 :  var t : array [a, b] of int;
2 :  J := b;
3 :  wh le (a < J) do
4 :    I := a;
5 :    wh le (I < J) do
6 :      f (t[I] > t[I + 1]) then
7 :        t[I] :=: t[I + 1]
8 :      fi;
9 :      I := I + 1
10 :     od;
11 :     J := J - 1
12 :   od
13 :   {s(t, a, b) ∧ a ≤ b}
```

³ Implementation by Pavol Černy.



A Practical Application of Abstract Interpretation to the Verification of Safety Critical Embedded Software

Reference

- [2] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. Design and implementation of a special-purpose static program analyzer for safety-critical real-time embedded software. *The Essence of Computation: Complexity, Analysis, Transformation. Essays Dedicated to Neil D. Jones*, LNCS 2566, pages 85–108. Springer, 2002.
- [3] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. A static analyzer for large safety-critical software. PLDI’03, San Diego, June 7–14, ACM Press, 2003.



A Parametric Specializable Static Program Analyzer

- C programs: safety critical embedded real-time synchronous software for non-linear control of very complex systems;
- 132,000 lines of C, 75,000 LOCs after preprocessing, 10,000 global variables, over 21,000 after expansion of small arrays;
- Semantics: ISO C99 + machine (IEEE 754-1985) + compiler + user;
- Implicit specification: absence of runtime errors, integer arithmetics should not wrap-around, etc;



The Class of Considered Periodic Synchronous Programs

```
declare volatile input, state and output variables;  
initialize state variables;
```

```
loop forever
```

- read volatile input variables,
- compute output and state variables,
- write to volatile output variables;

```
    wait_for_clock();
```

```
end loop
```

- The only allowed interrupts are clock ticks;
- Execution time of loop body less than a clock tick [4].

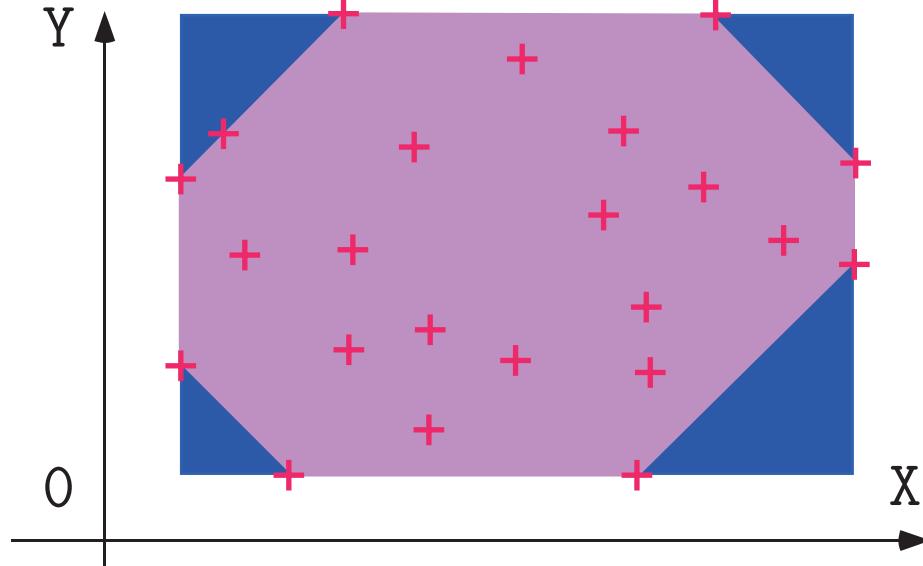
Reference

- [4] C. Ferdinand, R. Heckmann, M. Langenbach, F. Martin, M. Schmidt, H. Theiling, S. Thesing, and R. Wilhelm. Reliable and precise WCET determination for a real-life processor. *ESOP (2001)*, LNCS 2211, 469–485.



General-Purpose Abstract Domains: Intervals and Octagons





Intervals:

$$\begin{cases} 1 \leq x \leq 9 \\ 1 \leq y \leq 20 \end{cases}$$

Octagons [5]:

$$\begin{cases} 1 \leq x \leq 9 \\ x + y \leq 78 \\ 1 \leq y \leq 20 \\ x - y \leq 03 \end{cases}$$

Difficulties: many global variables, IEEE 754 floating-point arithmetic (in program and analyzer)

Reference

- [5] A. Miné. A New Numerical Abstract Domain Based on Difference-Bound Matrices. In *PADO'2001*, LNCS 2053, Springer, 2001, pp. 155–172.



Clock Abstract Domain

- Code Sample:

```
R = 0;  
while (1) {  
    if (I)  
        { R = R+1; }  
    else  
        { R = 0; }  
    T = (R>=n);  
    wait_for_clock ();  
}
```

- Output T is true iff the volatile input I has been true for the last n clock ticks.
- The clock ticks every s seconds for at most h hours, thus R is bounded.
- To prove that R cannot overflow, we must prove that R cannot exceed the elapsed clock ticks (*impossible using only intervals*).

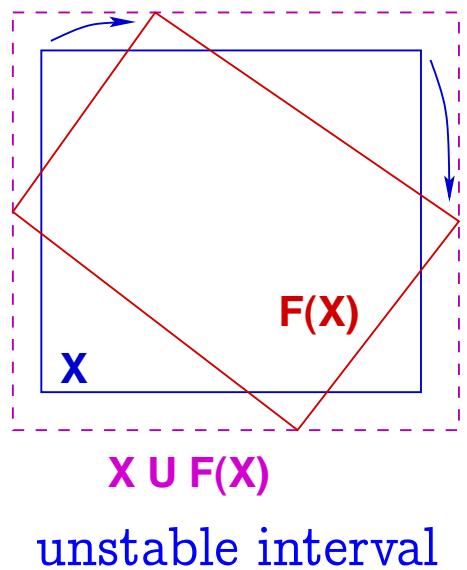
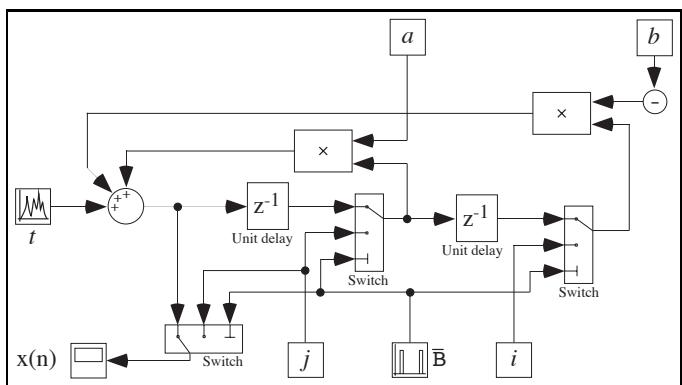
- Solution:

- We add a phantom variable clock in the concrete user semantics to track elapsed clock ticks.
- For each variable X, we abstract three intervals: X , $X+\text{clock}$, and $X-\text{clock}$.
- If $X+\text{clock}$ or $X-\text{clock}$ is bounded, so is X .

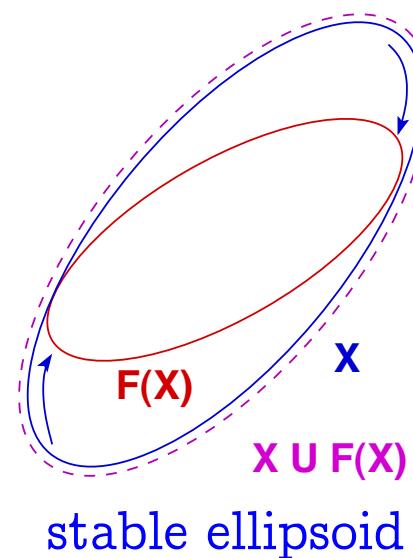


Ellipsoid Abstract Domain

2^d Order Filter Sample:



- Computes $X_n = \begin{cases} \alpha X_{n-1} + \beta X_{n-2} + Y_n \\ I_n \end{cases}$
- The concrete computation is bounded, which must be proved in the abstract.
- There is no stable interval or octagon.
- The simplest stable surface is an ellipsoid.



Example of Analysis Session

The screenshot shows the Visualizer tool interface with the following components:

- Toolbar:** quit, clocks, trees, octagons, filters, help.
- Search bar:** Search string: TRUC[0].
- Code Editor:** demo.c (highlighted). The code contains a snippet of C code involving variables P, X, TRUC[0], and TRUC[1].
- Output Window:** info (highlighted). It displays analyzer logs and constraints. Key log entries include:
 - /* Analyzer launched at 2003/6/2 11:45:43
 - 103.23142654533073426 <= X-P <= 166.32563104533073783 ;
 - 67.325631045330709412 <= X+P <= 202.23142654533074847 ;
 - >
 - <clock in {0}, <MACHIN in {0}>;
 - clock in {0};
 - <TRUC[0].e in {15.5}, TRUC[0].s in [-20.7485, 20.7485], TRUC[1].e in {15.5}, TRUC[1].s in [-20.7485, 20.7485], X in {15.5}, P in [-20.7485, 20.7485]
- Bottom Status:** coffee_machine_explosion 55.3 (ellipse)
L43 C21 c894



Benchmarks on real-size safety critical A340 code (100 000 LOCS)

- Comparative results (commercial software):
4,200 (false?) alarms,
3.5 days;
- Our results:
0 alarm,
80 mn on 2.8 GHz PC,
350 Megabytes.
- Can be done by predicate abstraction and model checking?



The main loop invariant

A textual file over 4.5 Mb with

- 6,900 boolean interval assertions ($x \in [0; 1]$)
- 9,600 interval assertions ($x \in [a; b]$)
- 25,400 clock assertions ($x + \text{clk} \in [a; b] \wedge x - \text{clk} \in [a; b]$)
- 19,100 additive octagonal assertions ($a \leq x + y \leq b$)
- 19,200 subtractive octagonal assertions ($a \leq x - y \leq b$)
- 100 decision trees
- 60 ellipse invariants, etc . . .

involving over 16,000 floating point constants (only 550 appearing in the program text) \times 75,000 LOCs.



Conclusion



Abstract Interpretation

- Abstract interpretation theory formalizes the idea of sound approximation for mathematical constructs involved in the specification of properties of computer systems.

References

- [POPL '77] P. Cousot & R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In *4th POPL*, pages 238–252, 1977.
- [Thesis] P. Cousot. *Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes*. Thèse d'État ès sciences mathématiques, Université scientifique et médicale de Grenoble, Grenoble, 21 Mar. 1978.
- [POPL '79] P. Cousot & R. Cousot. Systematic design of program analysis frameworks. In *6th POPL*, pages 269–282, 1979.
- [JLC '92] P. Cousot & R. Cousot. Abstract interpretation frameworks. *J. Logic and Comp.*, 2(4):511–547, 1992.



Applications of Abstract Interpretation

- **Static Program Analysis** [POPL '77,78,79] including **Dataflow Analysis** [POPL '79,00], **Set-based Analysis** [FPCA '95]
- **Syntax Analysis** [TCS 290(1) 2002]
- **Hierarchies of Semantics (including Proofs)** [POPL '92, TCS 277(1–2) 2002]
- **Typing** [POPL '97]
- **Model Checking** [POPL '00]
- **Program Transformation** [POPL '02]

All these techniques involve **sound approximations** that can be formalized by **abstract interpretation**



Conclusion on Verification by Abstraction

- Most applications of abstract interpretation tolerate a small rate (typically 5 to 15%) of false alarms:
 - Program transformation → do not optimize,
 - Typing → reject some correct programs, etc,
 - WCET analysis → overestimate;
- Some applications require no false alarm at all:
 - Program verification.
- Theoretically possible [SARA '00], practically feasible [PLDI '03]

Reference

[SARA '00] P. Cousot. Partial Completeness of Abstract Fixpoint Checking, invited paper. In *4th Int. Symp. SARA '2000*, LNAI 1864, Springer, pp. 1–25, 2000.

[PLDI '03] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. A static analyzer for large safety-critical software. PLDI'03, San Diego, June 7–14, ACM Press, 2003.



THE END, THANK YOU

More references at URL www.di.ens.fr/~cousot.



Seminario, Dipartimento di Informatica, Sala Verde, September 2nd, 2004

— 50 —

© P. Cousot

